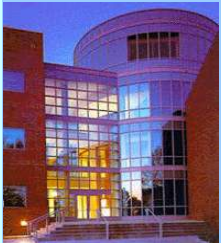


Introduction to:



Surface Science in Paper Recycling

Orlando J. Rojas presented and contributions by Richard A. Venditti

NC STATE UNIVERSITY

Department of Wood and Paper Science

ojrojas@ncsu.edu

www4.ncsu.edu/~ojrojas



Papermaking: A “Colloidal” Soup

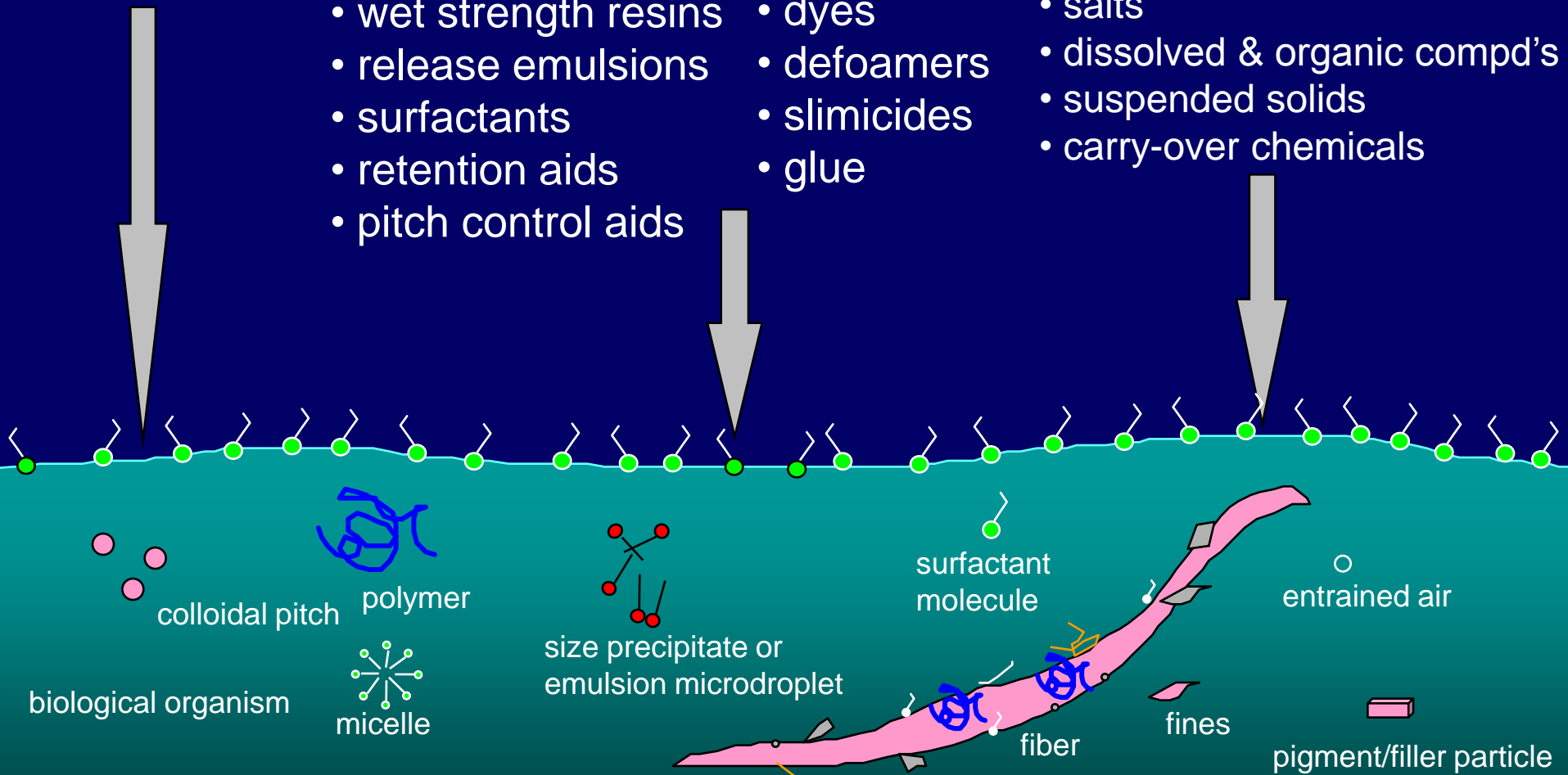
Pulping & Bleaching

Chemical Additives

Recycling & other process streams

- dry strength resins
- wet strength resins
- release emulsions
- surfactants
- retention aids
- pitch control aids
- promoters
- dyes
- defoamers
- slimicides
- glue

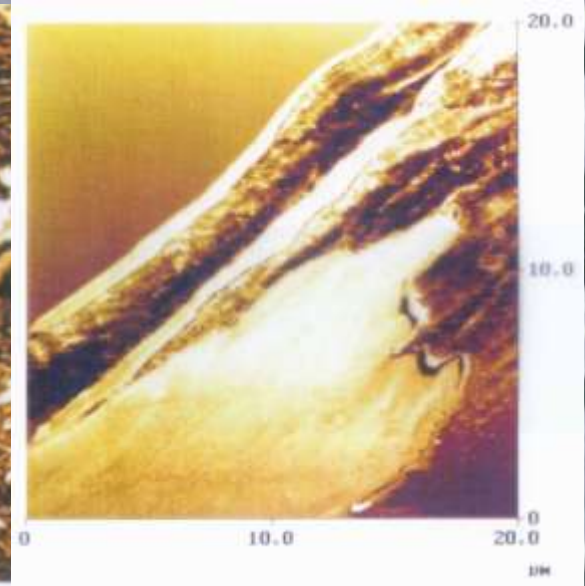
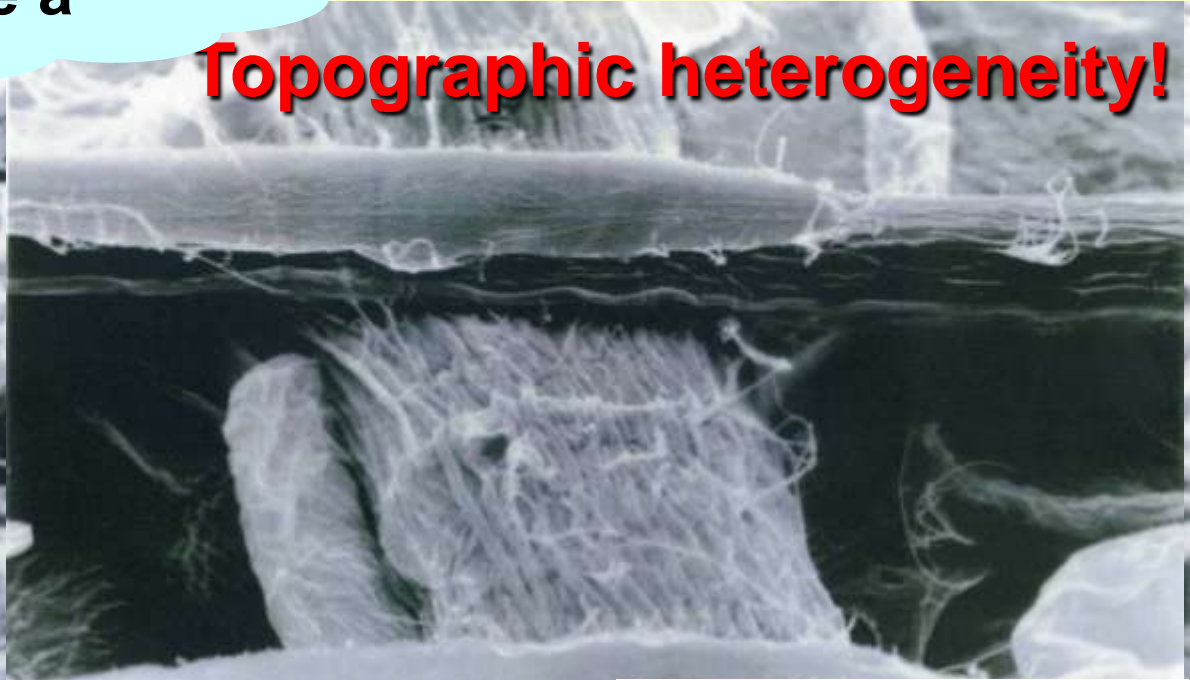
- salts
- dissolved & organic compd's
- suspended solids
- carry-over chemicals



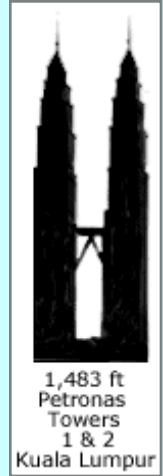
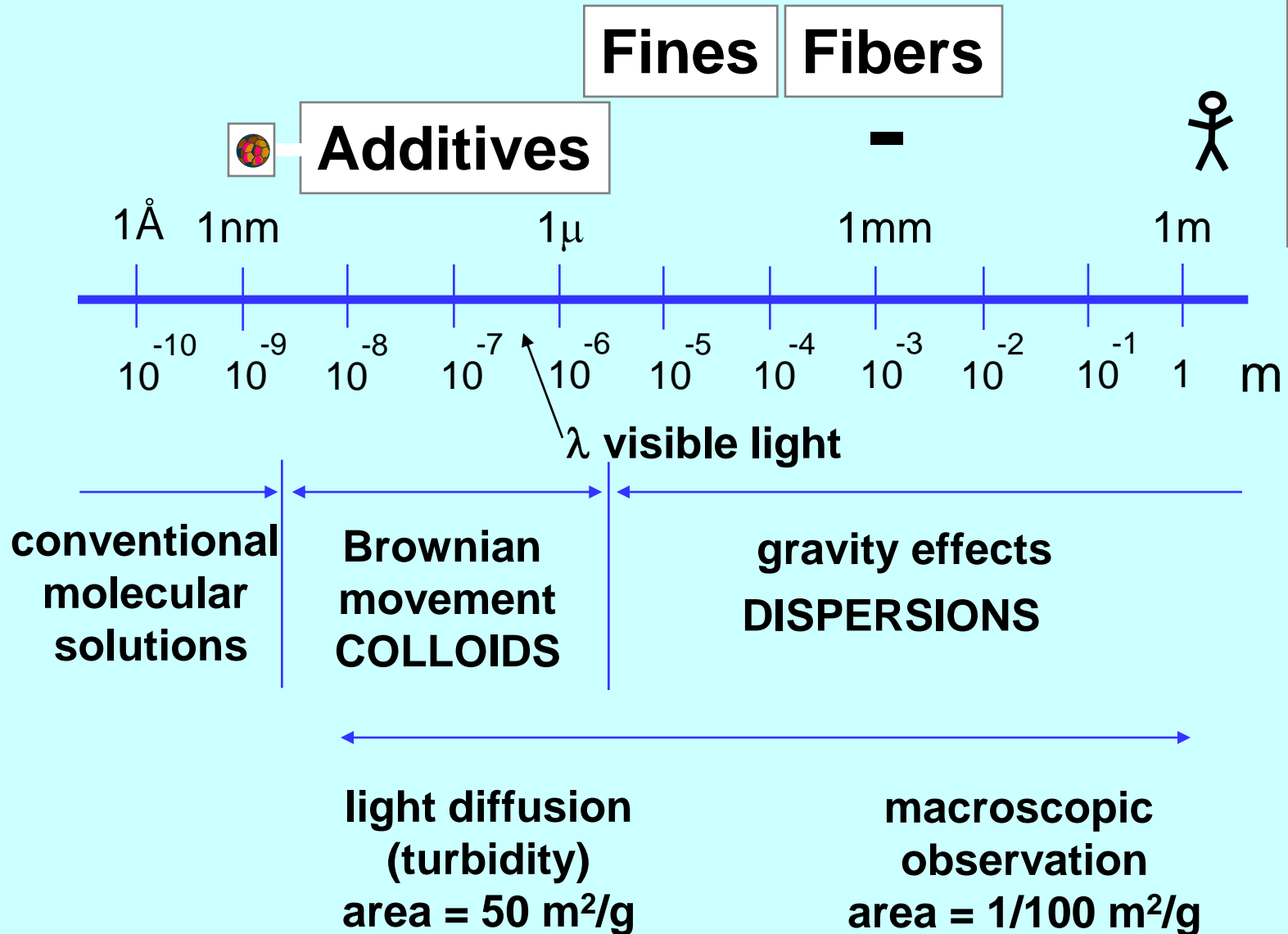
Papermaking Fibers

Let's take a tour

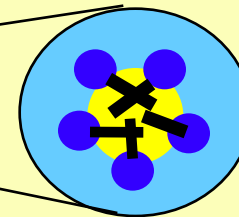
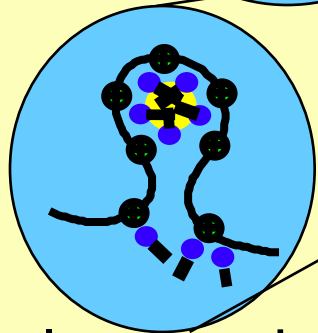
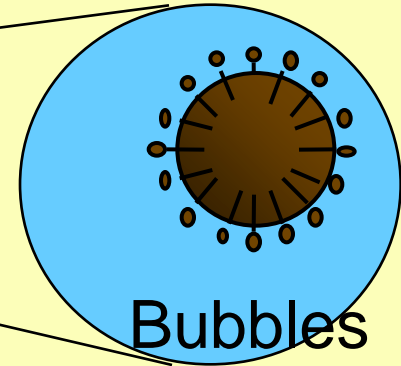
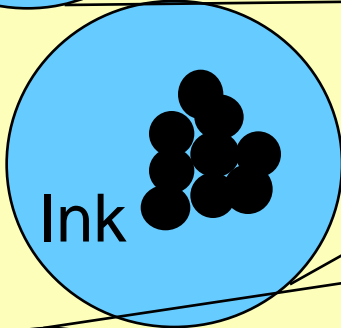
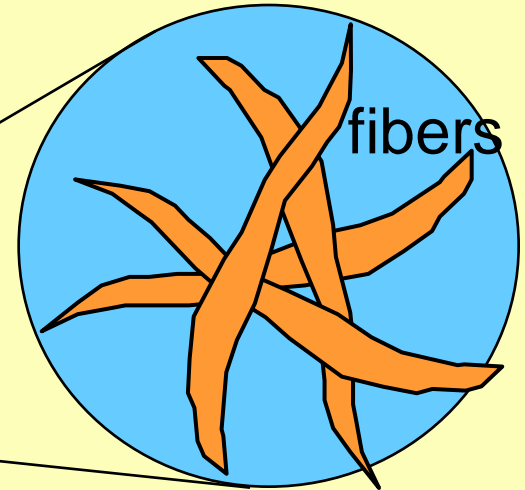
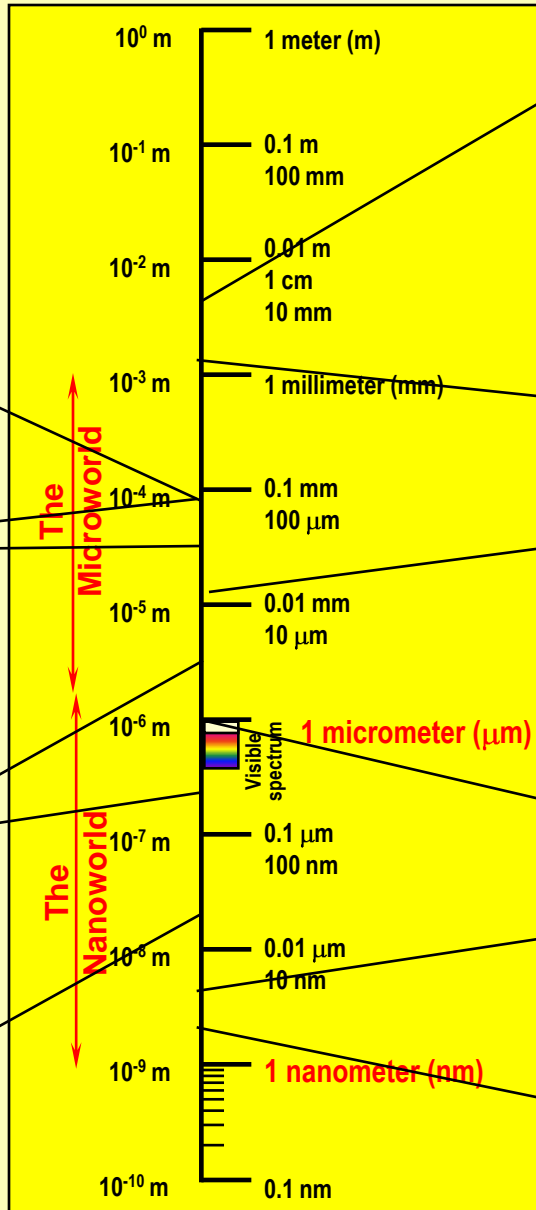
Topographic heterogeneity!



Sizes and Shapes



Colloids



Polymer-micelles

micelles

Deinking Chemicals

Sodium Hydroxide

Pulper – Bleaching

Sodium Silicate

Pulper – Bleaching

Chelating Agents

Pulper – Bleaching

Hydrogen Peroxide

Pulper – Bleaching

Surfactants

Pulper – Flotation - Washing

Collector Chemicals

Pulper – Flotation

Agglomeration Chemicals

Pulper – Cleaners

Calcium chloride

Flotation

Dispersants

Washing – Stock prep

Inks = complex formulations

Component	Function	Concentration, %
Deionized water	Aqueous carrier medium	60 - 90
Water soluble solvent	Humectant, viscosity control	5 - 30
Dye/pigment	Provides color	1 - 10
Surfactant	Wetting, penetrating	0.1 - 10
Biocide	Prevents biological growth	0.05 - 1
Buffer	Controls the pH of ink	0.1 - 0.5
Other additives	Chelating agent, defoamer, solublizer, etc.	> 1

Here we will talk about...

Surfaces

Surfactants



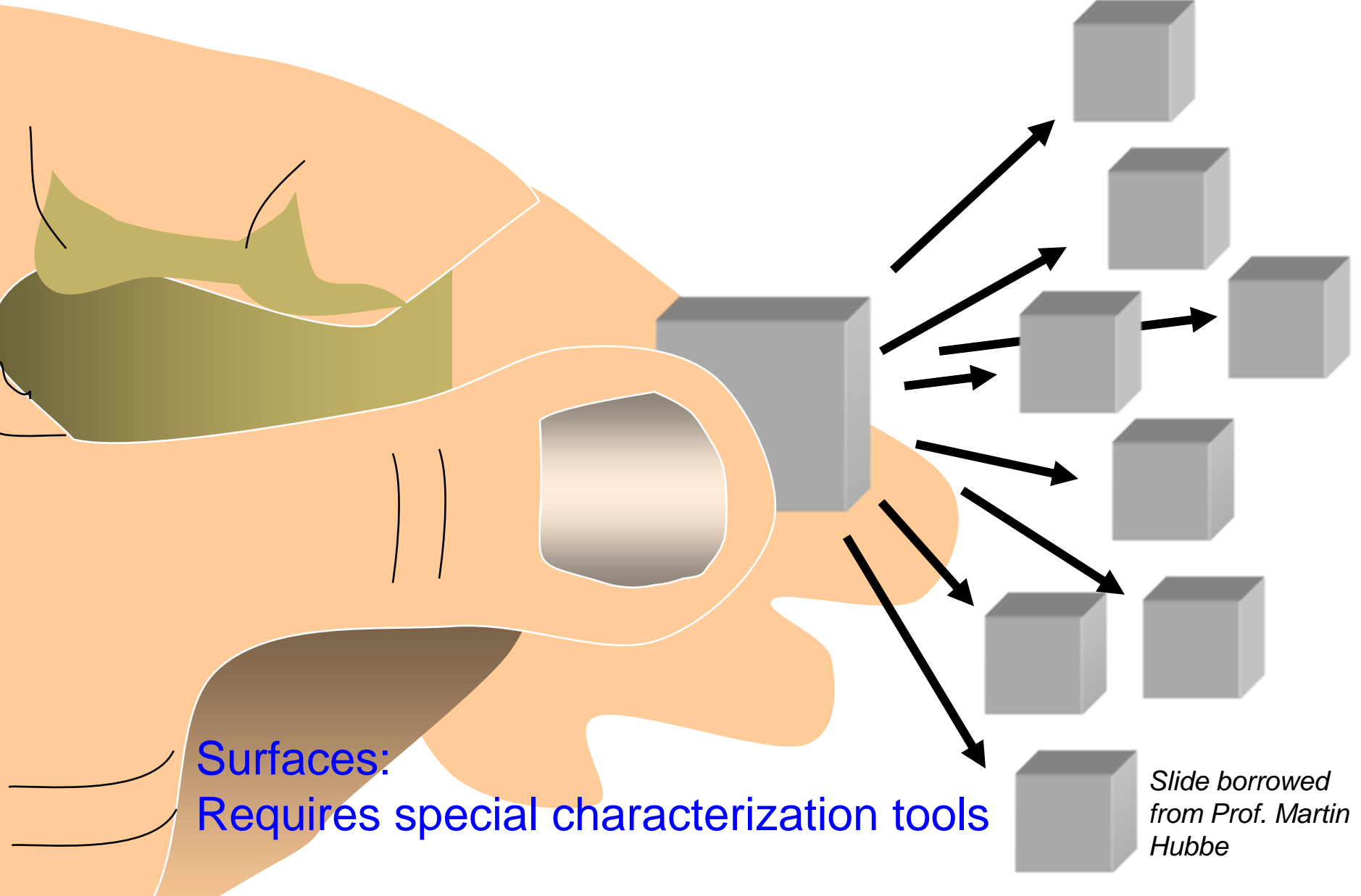
Surface energies

Contact angles

Water penetration

paper recycling, deinking, deposits, stickies, etc.

Surface area and particle size



Surfaces:
Requires special characterization tools

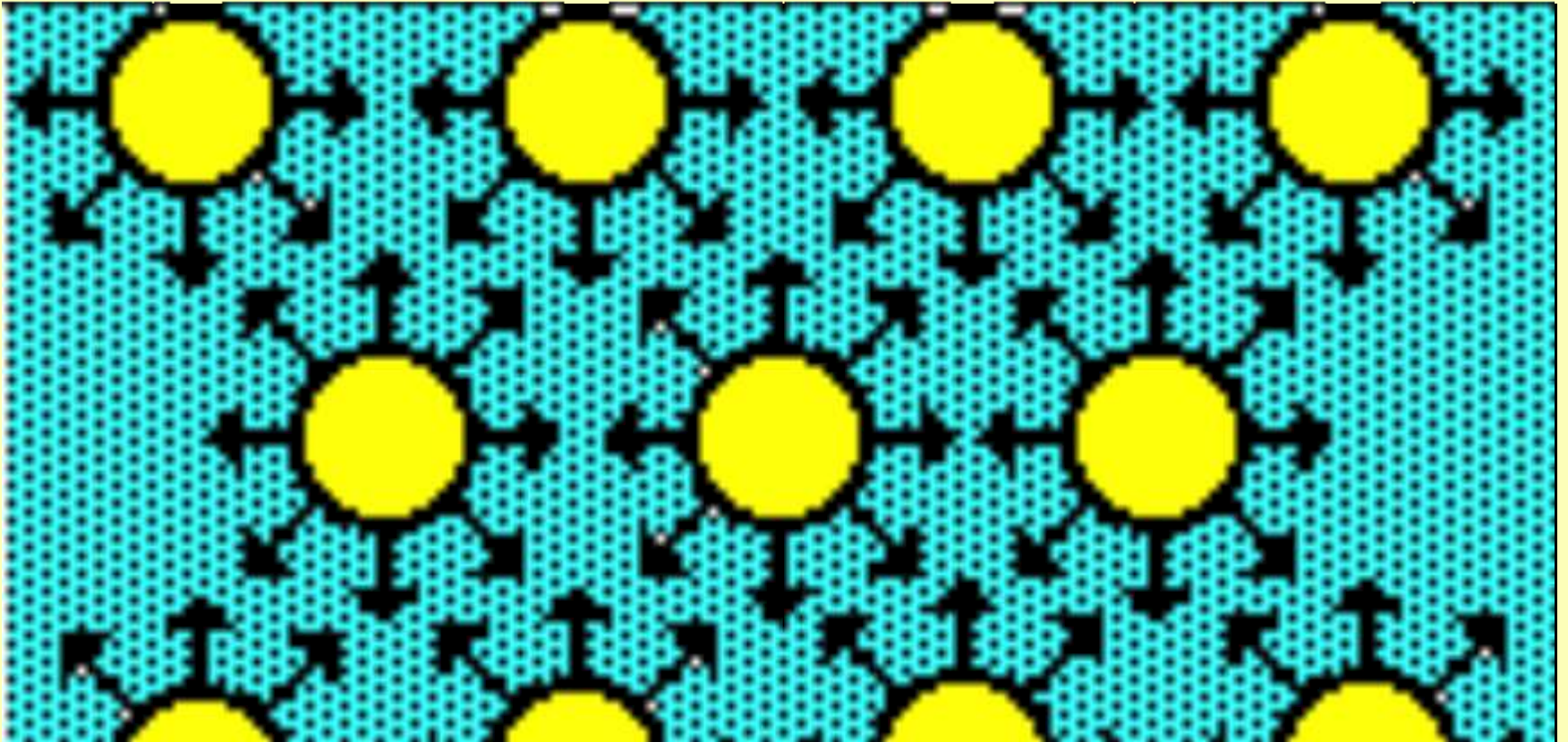
Slide borrowed from Prof. Martin Hubbe

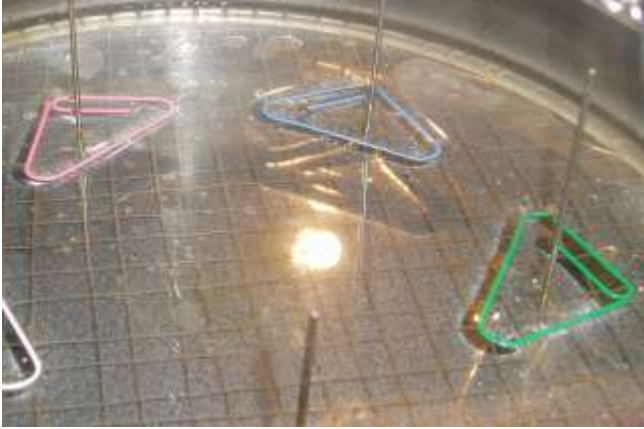
Surface and Interfacial Tension



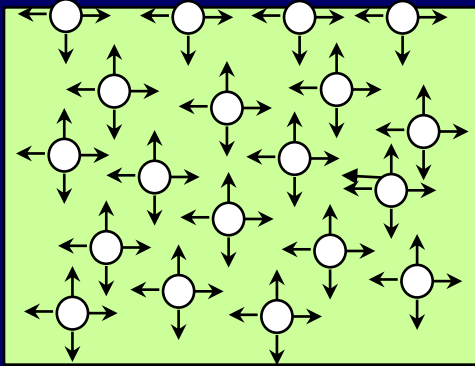
Surface Tension

- Surface net inward force





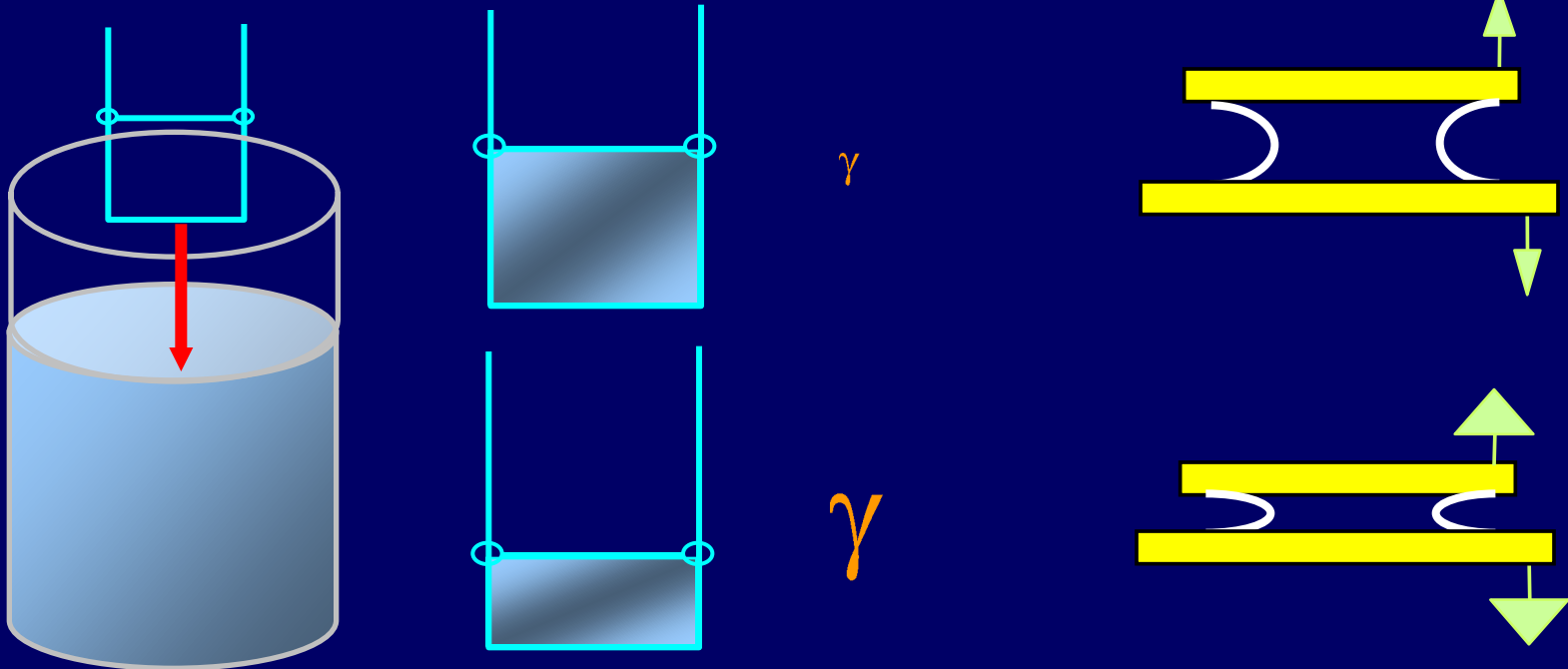
Surface Energy and Surface Tension (γ)



At surface: net “inward” force

Surface energy of a fluid... It is translated as the resistant to the creation of new surface area.

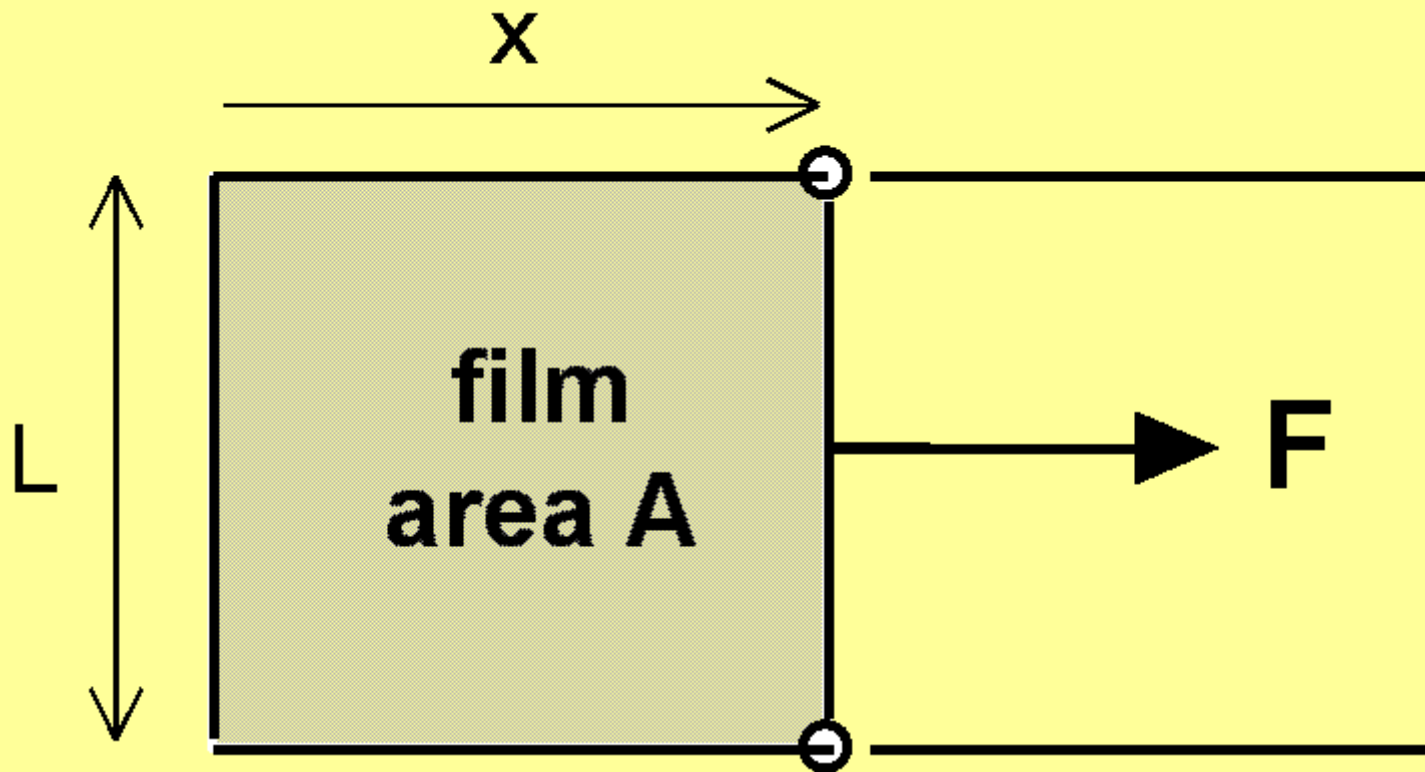
Unbalance of intermolecular forces exists at the liquid-air interface



Surface Energy

In nature every system tries to minimize its surface energy.

For example a drop of water in air will be spherical, not extended like a cylinder....



$$dx \longrightarrow dW = F dx$$

Force on the wire: $F = 2 \gamma L$ (2 sides)

$$dW = 2 \gamma L dx = \gamma dA$$

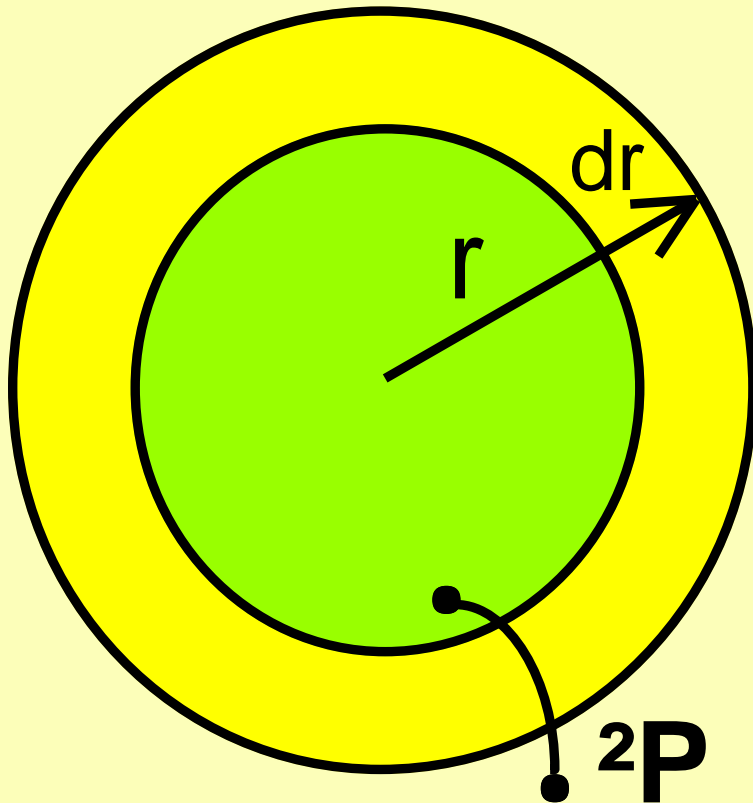
Mechanical Definition

$$\text{area } A = 4 \Pi r^2$$

$$dA = 8 \Pi r dr$$

Work against surface tension

$$dW = \gamma dA = 8 \Pi \gamma r dr$$

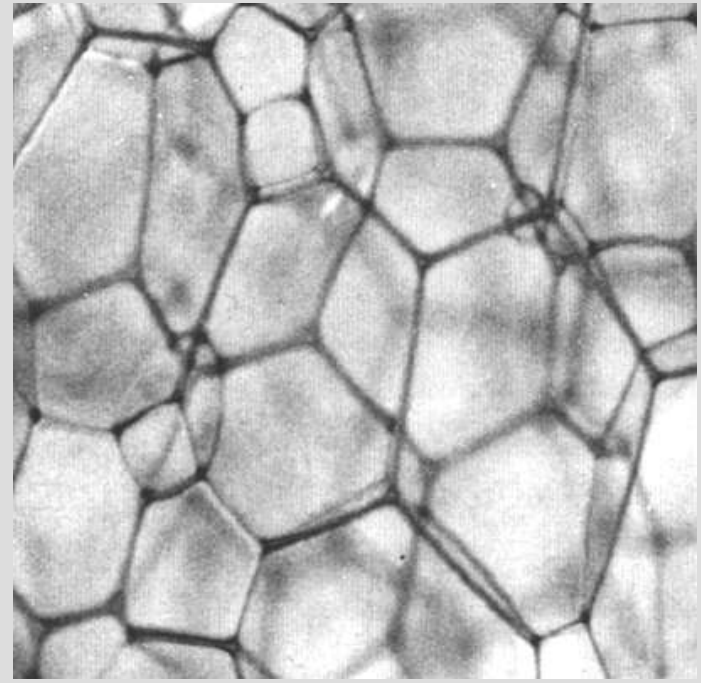
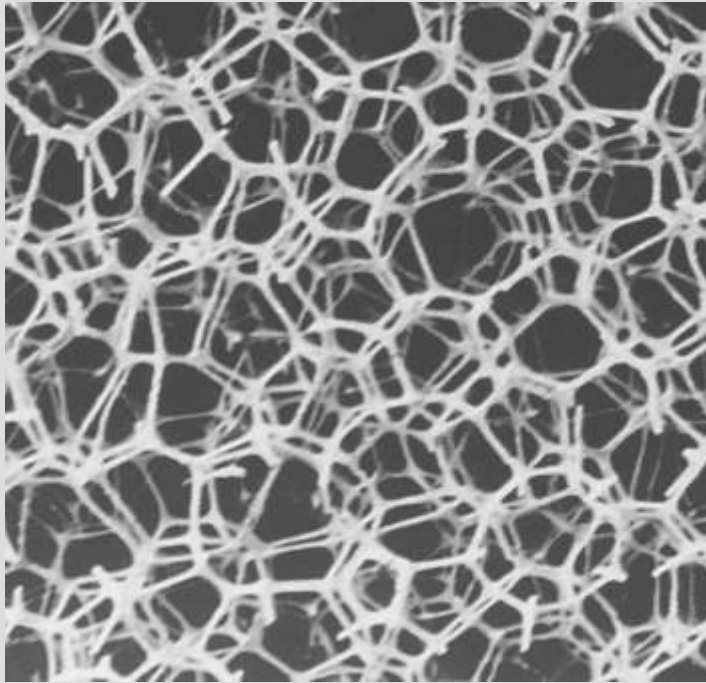


Work against Pressure

$$\begin{aligned} dW &= \Delta P dV = \Delta P A dr \\ &= \Delta P 4 \Pi r^2 dr \end{aligned}$$

Equating both expression for dW
Young-Laplace Eq. is obtained

$$\Delta P = 2\gamma / r$$

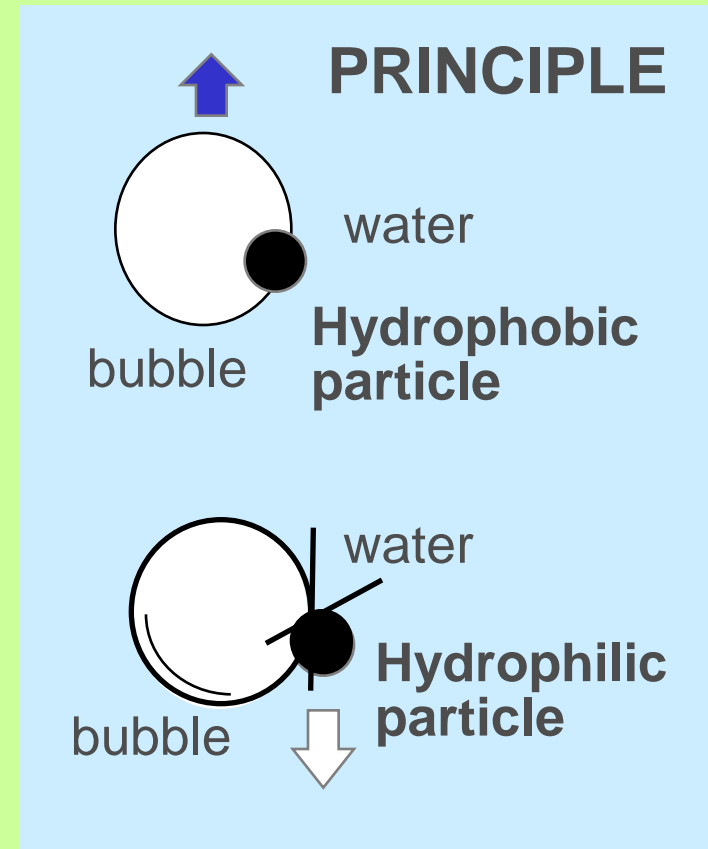
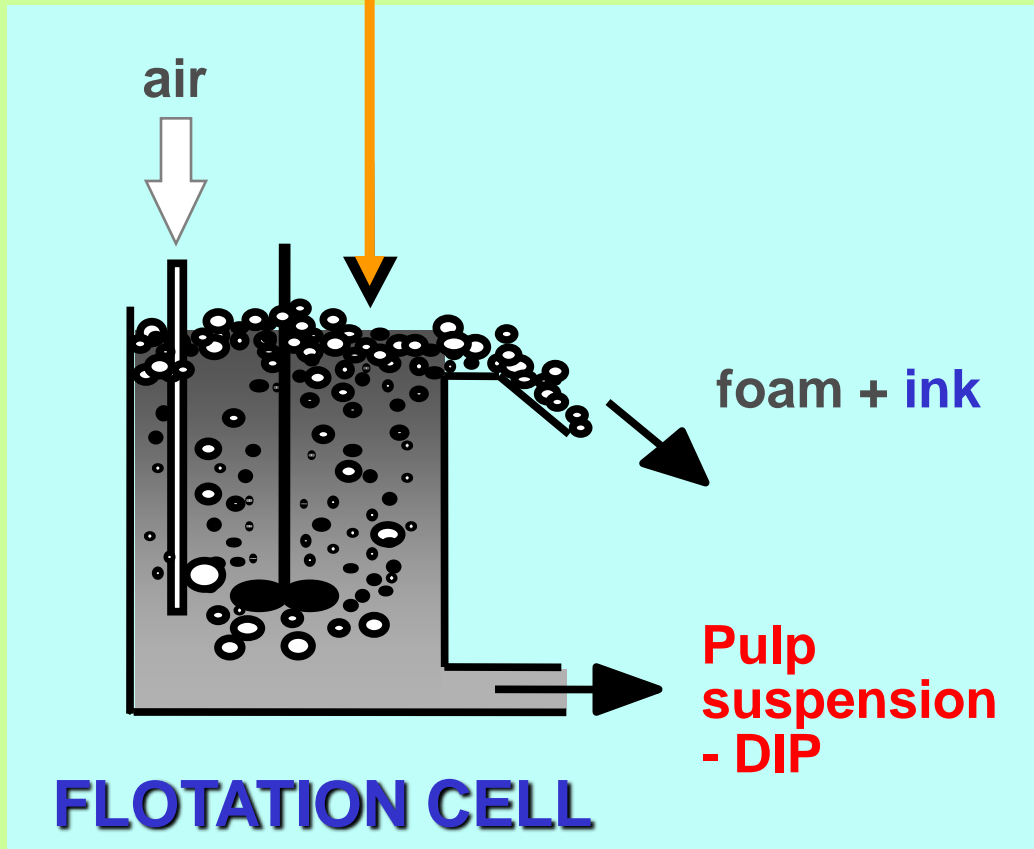


**solid and liquid foams: can be formed from
low Surface tension media**

Flotation

Hydrophobic particles (pigments)

...





Surface Tensions of Some Pure Liquids at 293 K

<i>Substance</i>	<i>γ (mN/m)</i>
Acetone	23.7
Benzene	28.8
Carbon Tetrachloride	27.0
Methylene Iodide	50.8
Water	72.8
Methanol	22.6
n-Hexane	18.4

Organic molecules with **polar groups** such as iodide and hydroxyl have a slightly lower surface energy than **water**.

Pure **hydrocarbons** are even lower, while **fluorinated** compounds are very low because the fluorine atom won't share electrons very well so only dispersion interactions occur.



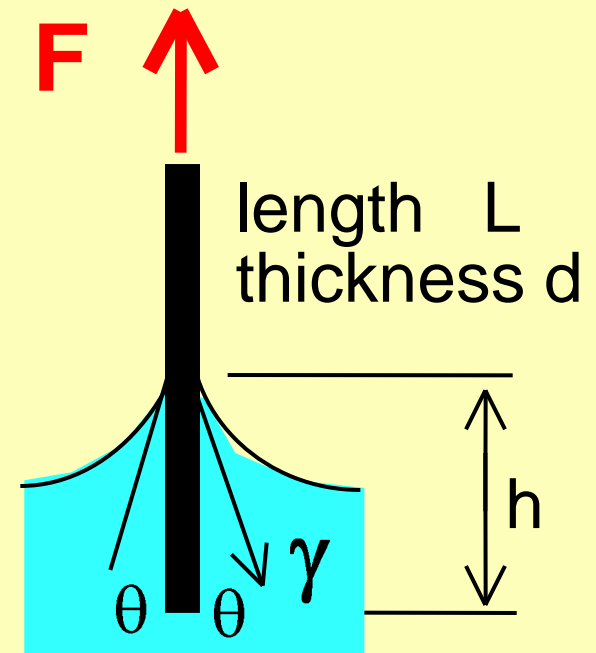
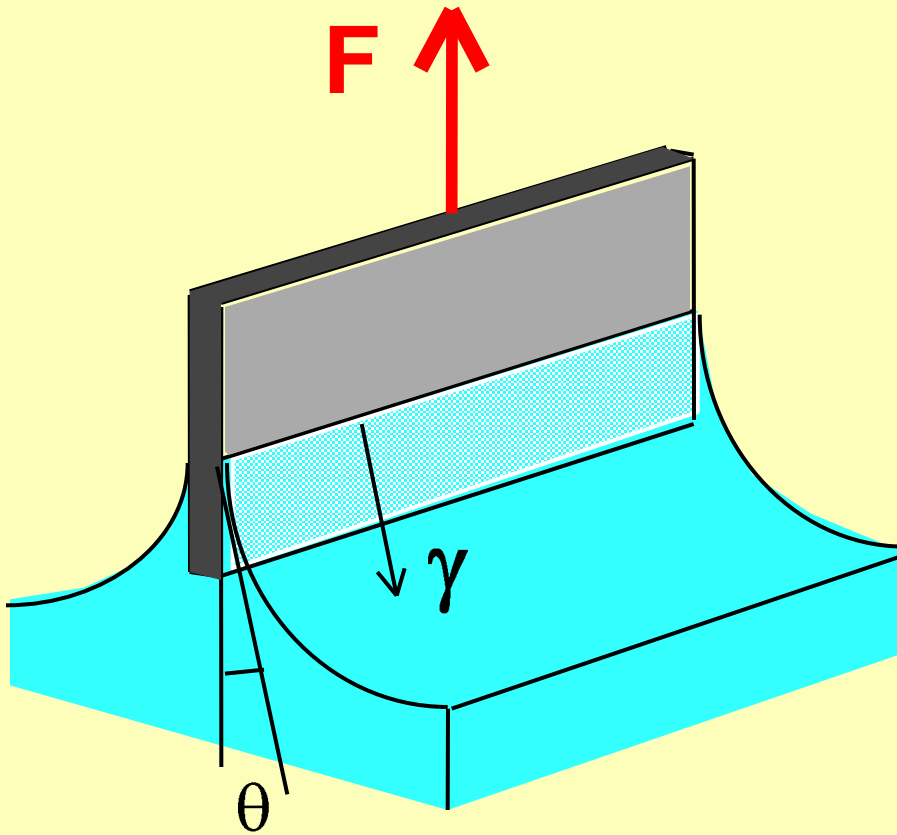
Surface Tension Measurement

Surface Tension Measurement

3 methods

- **Force measurement**
- **Pressure measurement**
- **Deformation measurement**

Wilhelmy Plate



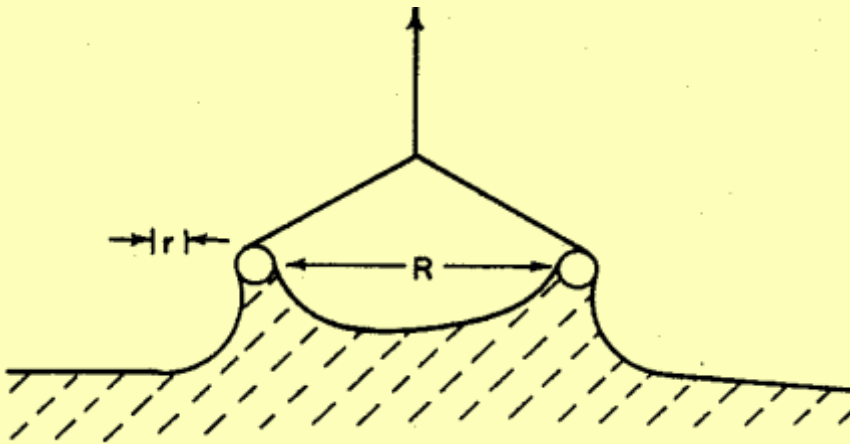
$$F = 2(L + d)\gamma \cos \theta$$

↑

2 sides

du Noüy Ring Method

To Balance



Adamson & Gast (1997)

Detachment Method

$$W_{\text{total}} = W_{\text{ring}} + 4\pi R\gamma_{\text{obs}}$$

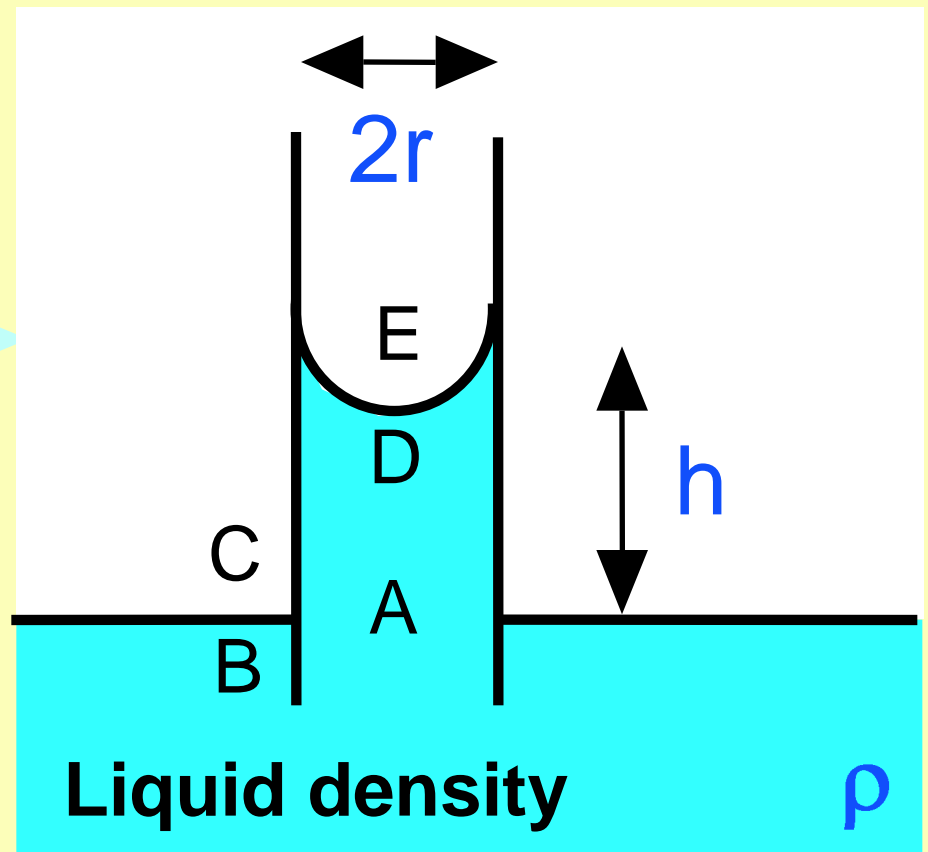
Correction due to width of ring material

$$\gamma_{\text{true}} = f \cdot \gamma_{\text{obs}}$$

where $f = f(R^3/V, R/r)$ [V = meniscus volume]

Capillary Rise

$$\rho g h = \frac{2 \gamma}{r}$$



Methods for Measuring γ

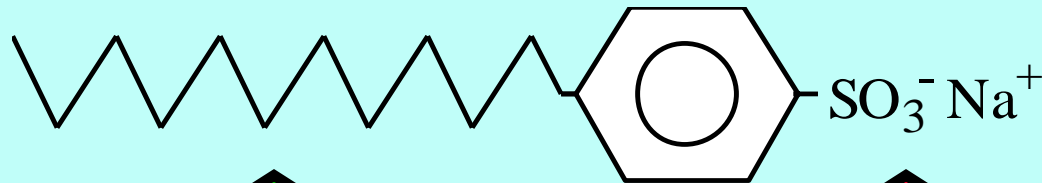
<u>Method</u>	<u>Pure Liquids</u>	<u>Solutions</u>
✓ Capillary Rise	Good when liquid wets reproducibly	Difficult
Sessile Drop	Good	Good for aging effects
Pendant Drop	Satisfactory, but has expt'l difficulties	Good for studying aging effects
✓ Wilhelmy Plate	Accurate, convenient with good set-up	Good, including aging effects
Maximum pull on cylinder	Good, easy to operate and simple apparatus	Satisfactory if used with care
✓ du Noüy Ring	Satisfactory	Unsatisfactory
✓ Drop Weight	Good	Poor if aging effects expected
Max. Bubble Pressure	Satisfactory when others impractical	Poor if aging effects expected

Surfactants



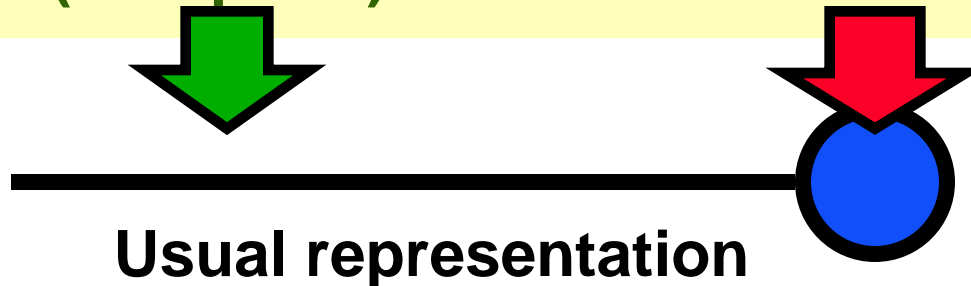
Surfactant = Amphiphile

Sodium Dodecyl benzene sulphonate



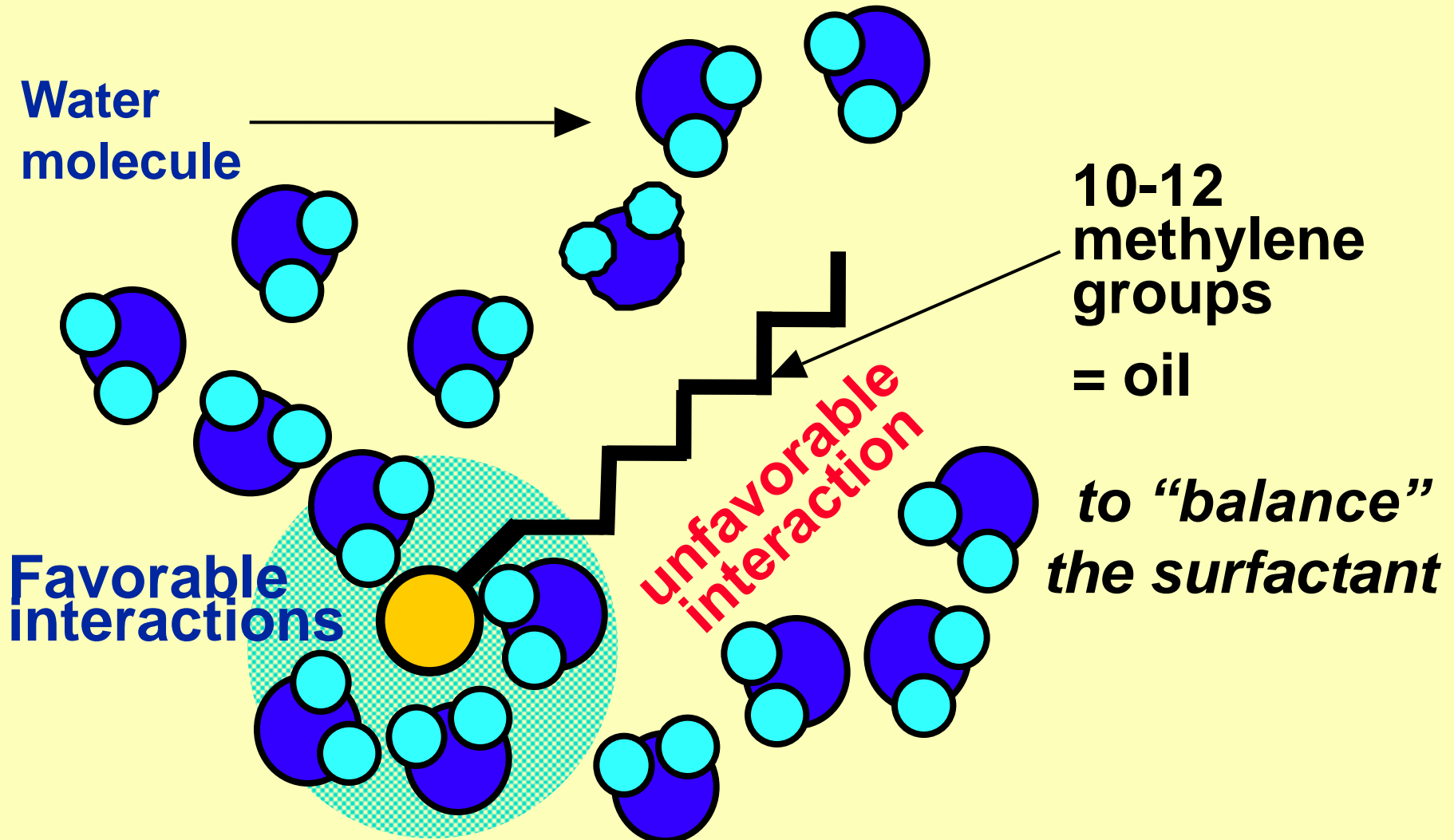
Hydrophobic Group
Lipophilic
(non-polar)

Hydrophilic Group
(polar)



In aqueous solution

Favorable & unfavorable Interactions



Surfactants

Amphiphilic nature



hydrophilic

(lipophobic)

hydrophobic

(lipophilic)

Classification according to head-group:

- Anionic
- Cationic
- Nonionic
- Zwitterionic

*****(See hand out)***

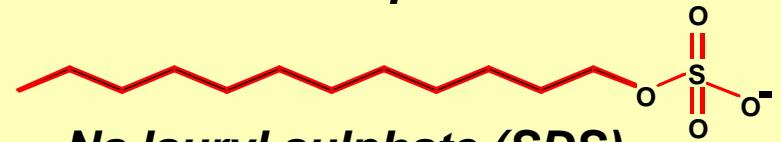
Anionic surfactants

- **Largest group of surfactants**
(~65% world market)
- **Sensitive to electrolytes (salt and Ca²⁺)**
- **Sulphates hydrolyse at low pH, otherwise chemically stable**
- **Soaps still important (foam and washing)**
- **Alkylether sulphates, lower cmc, compatible low pH and high hardness.**
- **Phosphate esters; good wetting agents, corrosion inhibitors, antistatic properties**

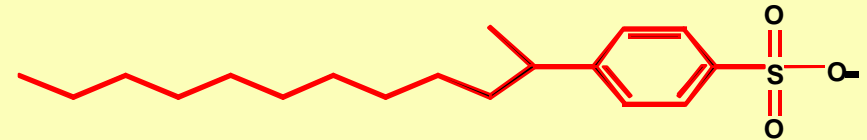
Biodegradable under aerobic conditions
Shampoos, handsoaps, laundry detergents



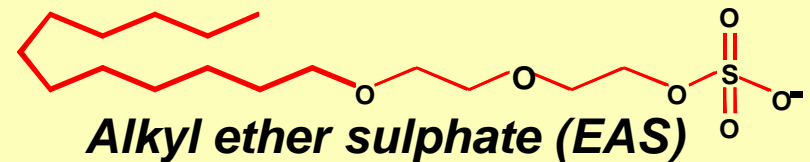
soap



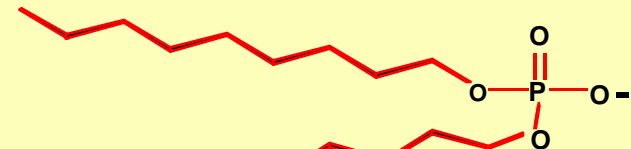
Na lauryl sulphate (SDS)



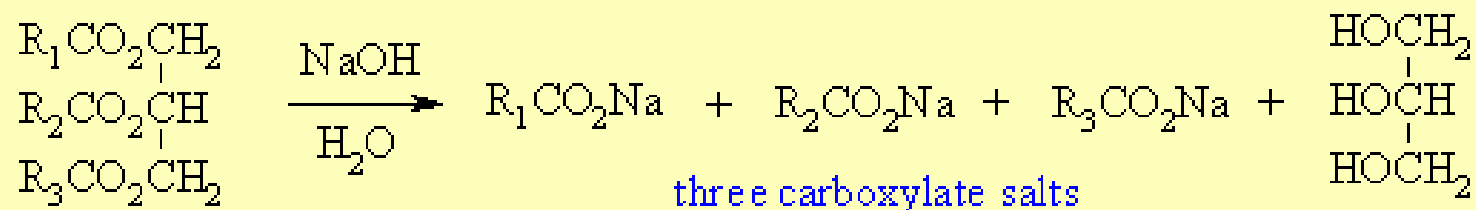
Linear alkyl benzene sulphonate (LABS)



Alkyl ether sulphate (EAS)



Phosphate ester



C12-C20 saturated acids

$CH_3(CH_2)_{10}CO_2H$	lauric acid
$CH_3(CH_2)_{12}CO_2H$	myristic acid
$CH_3(CH_2)_{14}CO_2H$	palmitic acid
$CH_3(CH_2)_{16}CO_2H$	stearic acid
$CH_3(CH_2)_{18}CO_2H$	arachidic acid

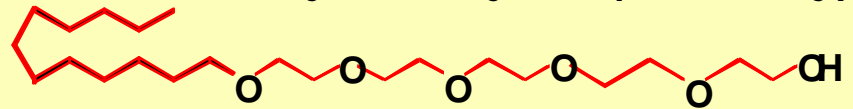
C18 unsaturated acids:

$CH_3(CH_2)_7CH=CH(CH_2)_7CO_2H$	oleic acid
$CH_3(CH_2)_4(CH=CHCH_2)_2(CH_2)_6CO_2H$	linoleic acid
$CH_3CH_2(CH=CHCH_2)_3(CH_2)_6CO_2H$	linolenic acid

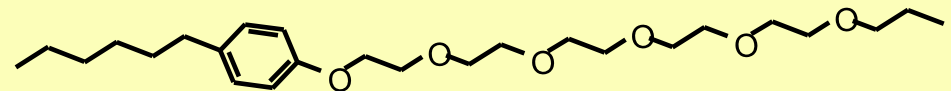
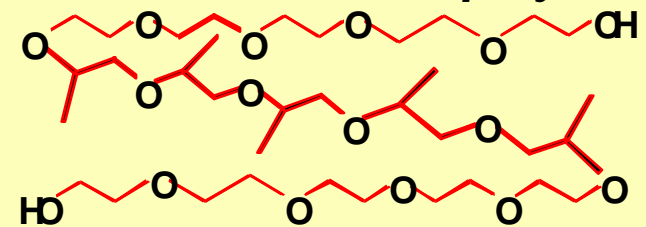
Non-ionic surfactants

- **Second largest group of surfactants** (~25% world market)
- **Dominated by polyoxyethylene products**
- **Not sensitive to salts (e.g. Ca^{2+})**
- **Temperature sensitive: water solubility reduced at higher T**
- **Much lower cmc than nonionic surfactants; efficient at low concentrations**

Alkyl ethoxylate (AE, C_xE_y)



EO-PO blockpolymer



(Joy dish soap)

Spans (Sorbitan Esters)

Tweens (Polyoxyethylene Sorbitan Esters)

Smooth rinsing (no water spots)

Dish soaps, window washers, insecticides

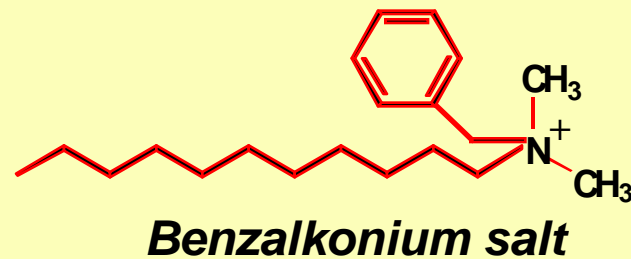
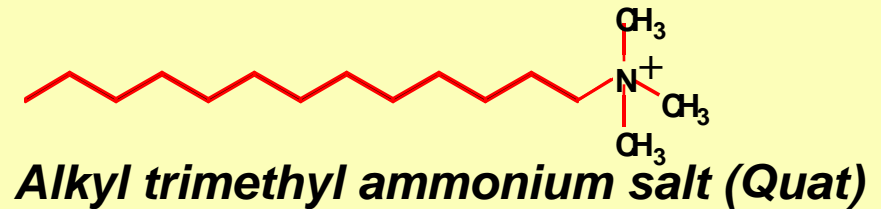
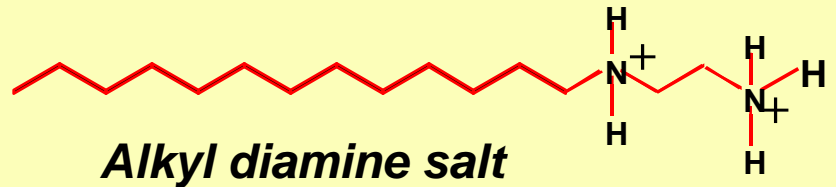
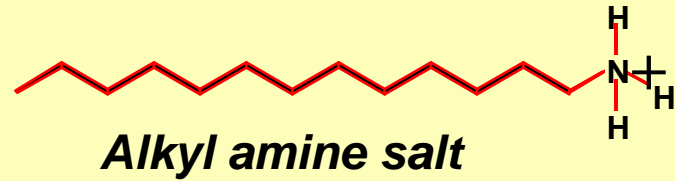
Cationic surfactants

(~10% world market)

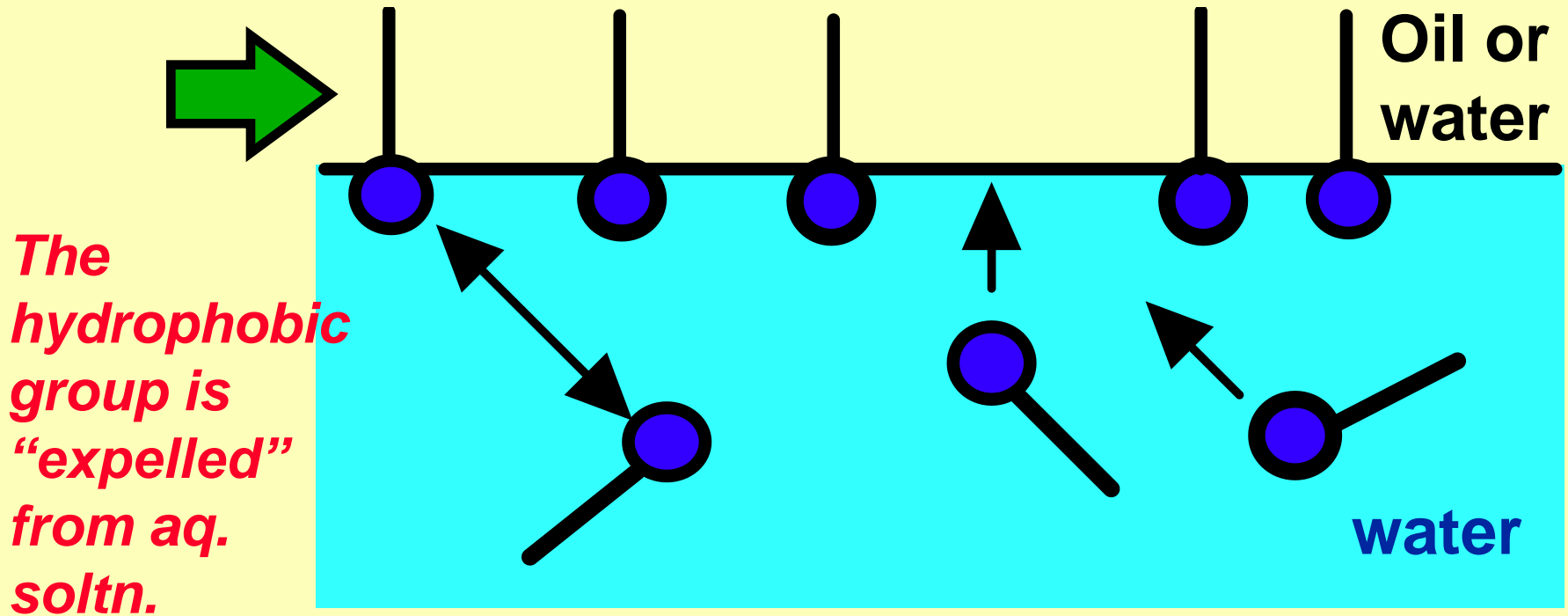
- Composed of a quaternary amino group as cationic head
- Not compatible with anionic surfactants
- Adsorbs strongly to many surfaces
- Used to modify a surface properties:

Textile softener
Adhesion promoter
Corrosion inhibitor
Anticaking agent
Mineral flotation

- Counter ions: halides (Cl⁻, Br⁻) or organic (MeSO₄⁻)

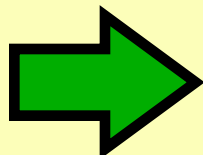


Surface or Interfacial Adsorption

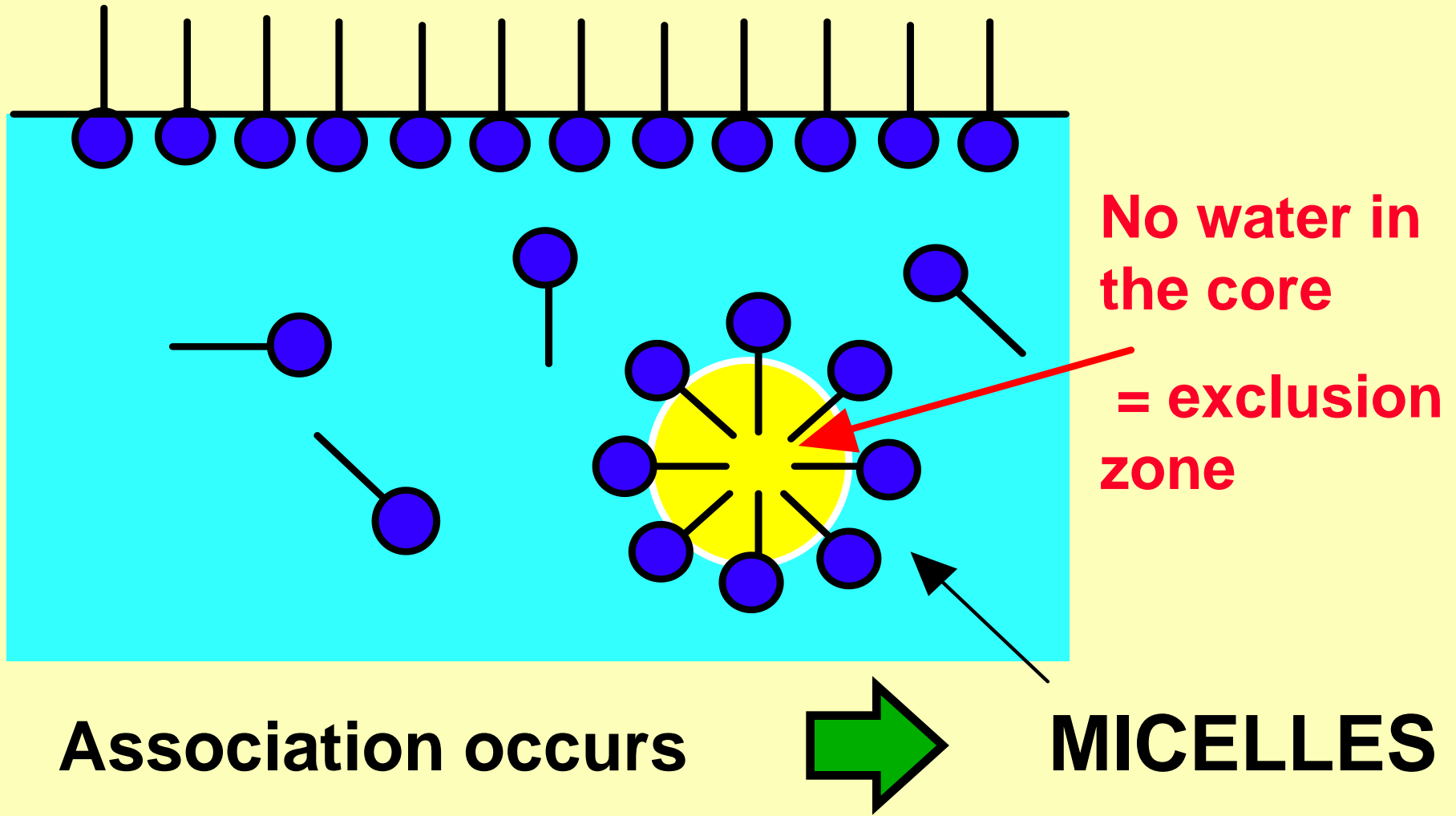


First added molecules ...

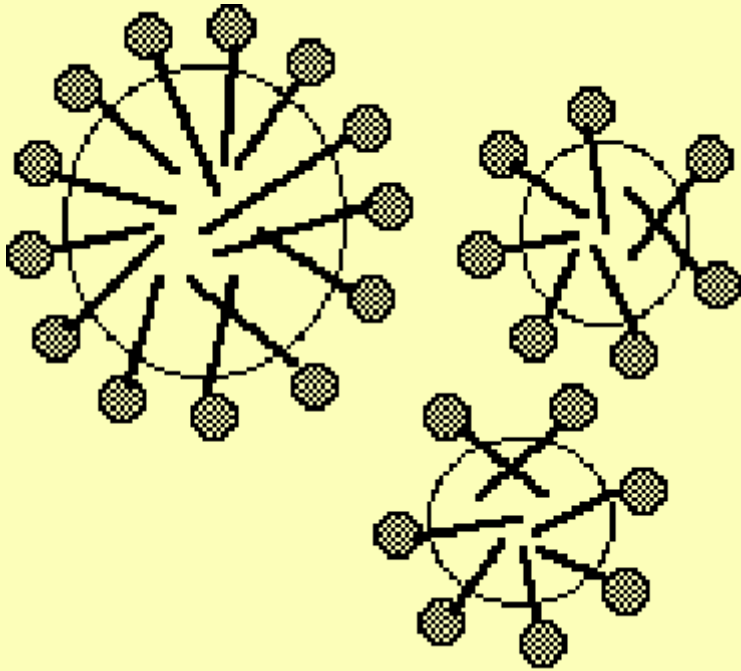
... In aqueous solution

 are adsorbed at the surface or interface

When the surface is saturated...



MICELLE = aggregation colloid



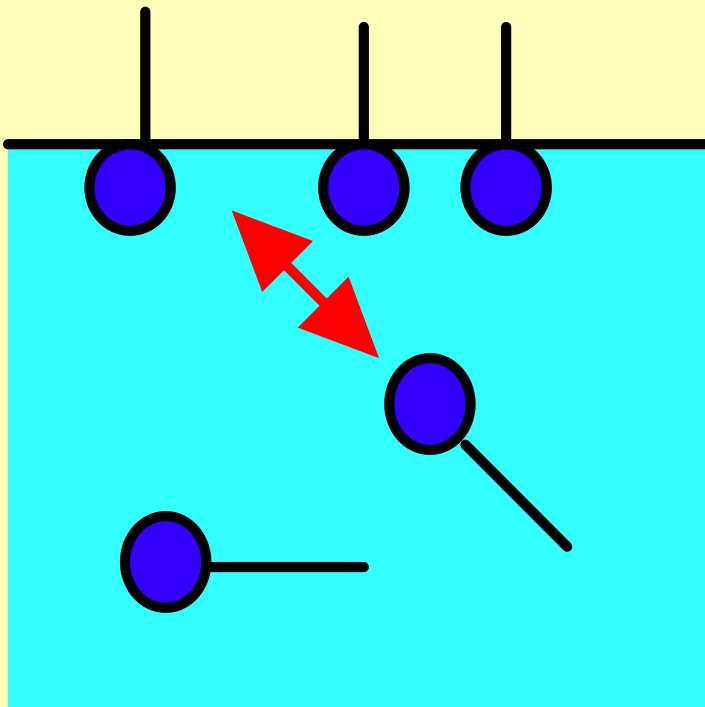
- size \pm 20 - 50 Å depending on surfactant
- Aggregation number 50-100 molecules
- Spherical form \pm depending on medium
- cylindrical, elongated, spaghetti ...

Surface Activity



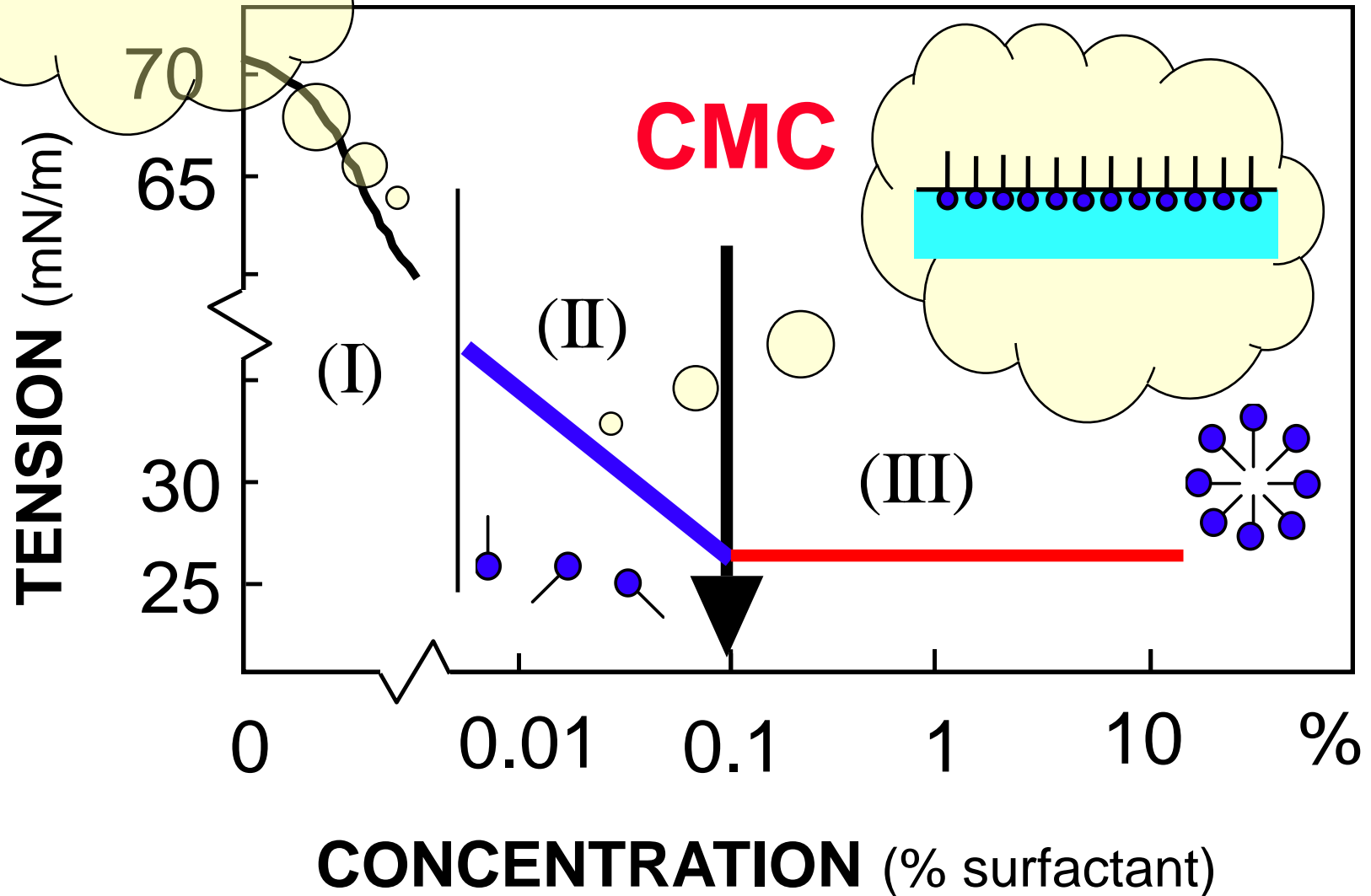
Surface Activity

Tension (= free energy per unit area) is linked to ...



- **Surface adsorption**
- **surface concentration**

Surface Tension - Concentration



Surfactants

- Because they have both Hydrophilic and lipophilic parts they are compatible at surfaces
- This lowers surface energy of the system
- **Enables foaming!!**

- But **be careful**, surfactant will also attach to hydrophobic contaminants making them more stable in water
 - Bad for flotation
 - Good for anti-deposition
 - Good for washing

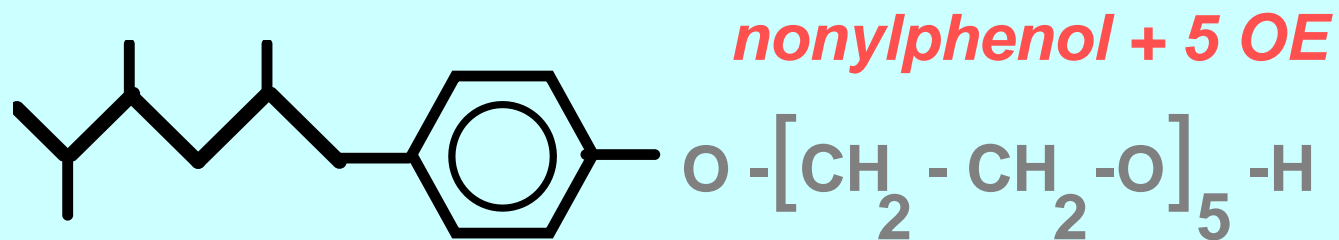
Simple Surfactant Characterization Parameter: HLB

- **Hydrophilic to lipophilic balance**

HLB calculated from empirical formula

- *for instance* - ethoxylated nonionics

$$\text{HLB} = 1/5 \text{ of polyether wt. \%}$$

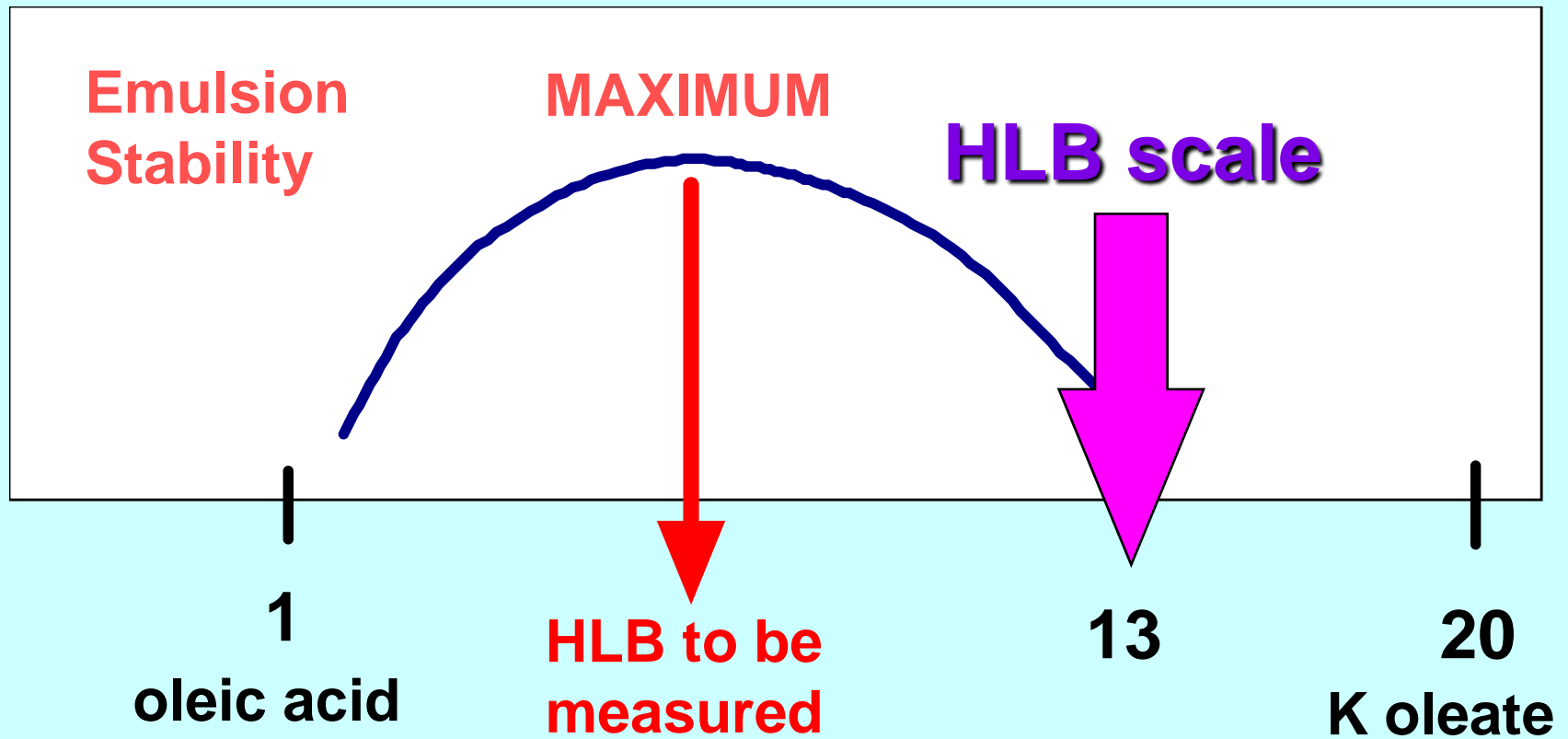


$$\text{HLB} = \frac{1}{5} \frac{44 \times 5}{220 + 44 \times 5} \times 100 = \mathbf{10}$$

HLB

Griffin 1949

- original method based on the
- stability of O/W emulsions
- tedious and inaccurate



HLB can be related to structure

- Davies' relationship (1957)

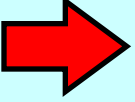
$$\text{HLB} = 7 + \begin{array}{l} \text{contributions} \\ \text{of hydrophilic} \\ \text{groups} \end{array} - \begin{array}{l} \text{contributions} \\ \text{of lipophilic} \\ \text{groups} \end{array}$$

Contribution values

-SO ₄ Na	+ 39	-COOH	+ 2,1	>CH-	- 0,5
-COOK	+ 21	-OH	+ 2,0	-CH ₂ -	- 0,5
-COONa	+ 19	- O -	+ 1,3	-CH ₃	- 0,5

Davies J. T., A quantitative kinetic theory of emulsion type. I. Physical chemistry of the emulsifying agent, *Gas/Liquid and Liquid/Liquid Interfaces. Proceedings 2nd Intern. Congress Surface Activity*, volume I, pag 426-438, Butterworths, London (1957)

HLB

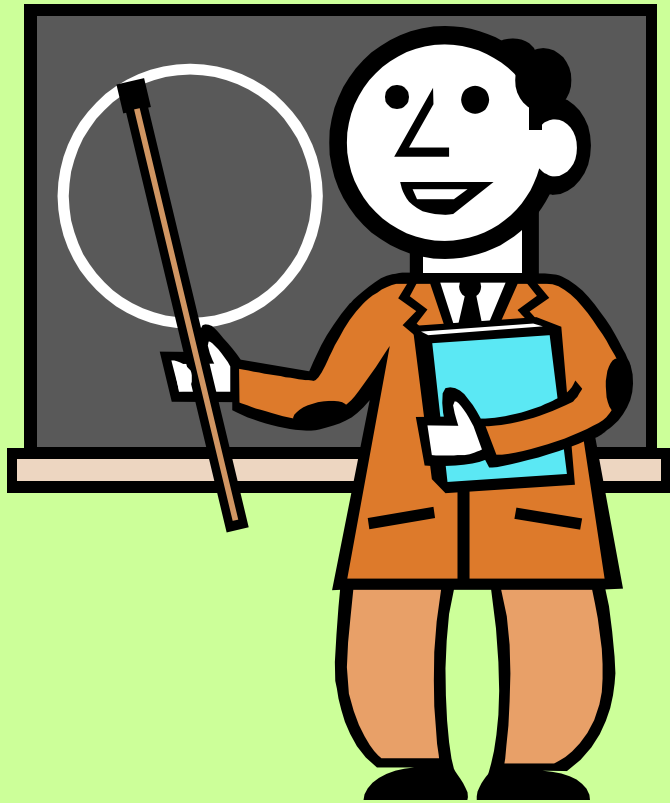
main advantage is  **its simplicity**
but ...

- to be used with caution (± 2 units)
- as a property of the surfactant only
- varies with temperature and other factors

*useful to compare surfactants in a same
physico-chemical environment !!!*

Critical Micelle Concentration

CMC



how to measure it and
how it can be affected

CMC micelle critical concentration can be detected in many ways

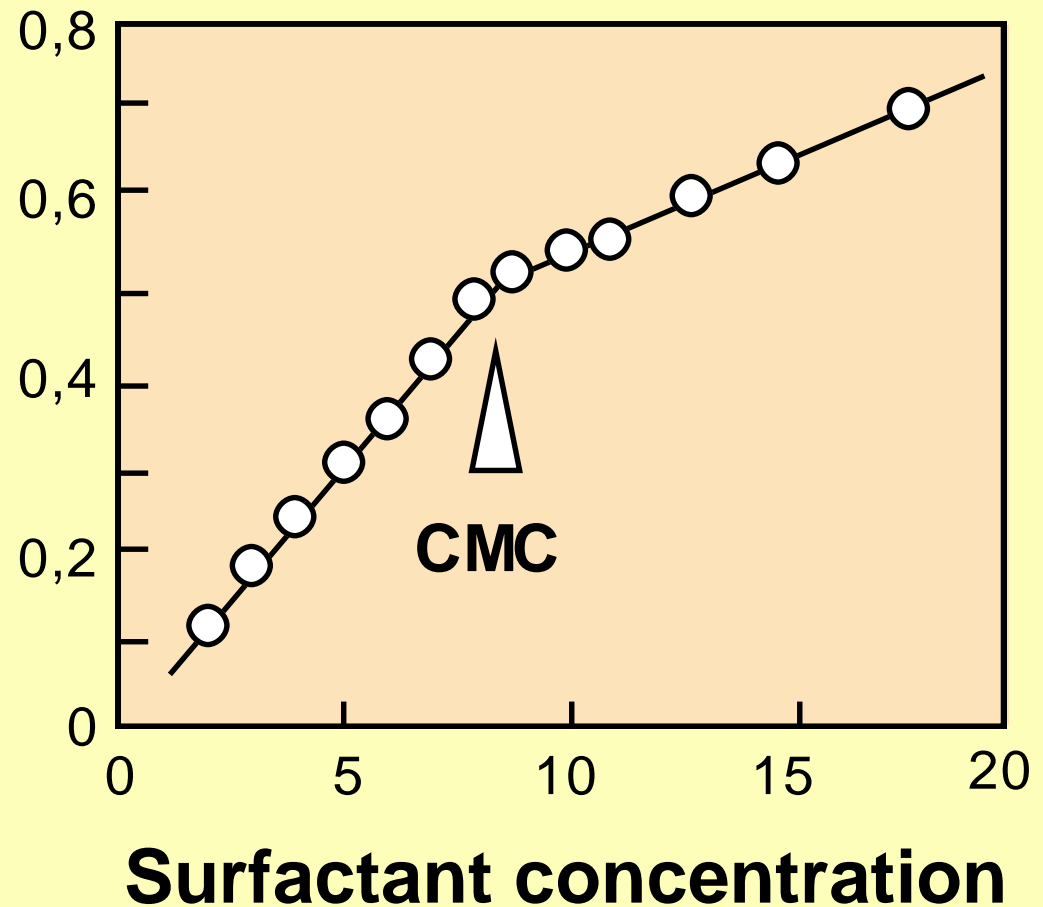
- **Surface/interface tension**
- **Electrolytic conductivity (ions)**
- **Osmotic pressure, Cryoscopy**
- **Dye solubilization**
- **Laser scattering (laser) and light diffraction (X-rays (SAXS), neutrons (SANS))**
- **Solubility of an apolar probe, NMR, UV/Vis**

CMC

- **Electrolytic conductivity (ionic surfactants)**

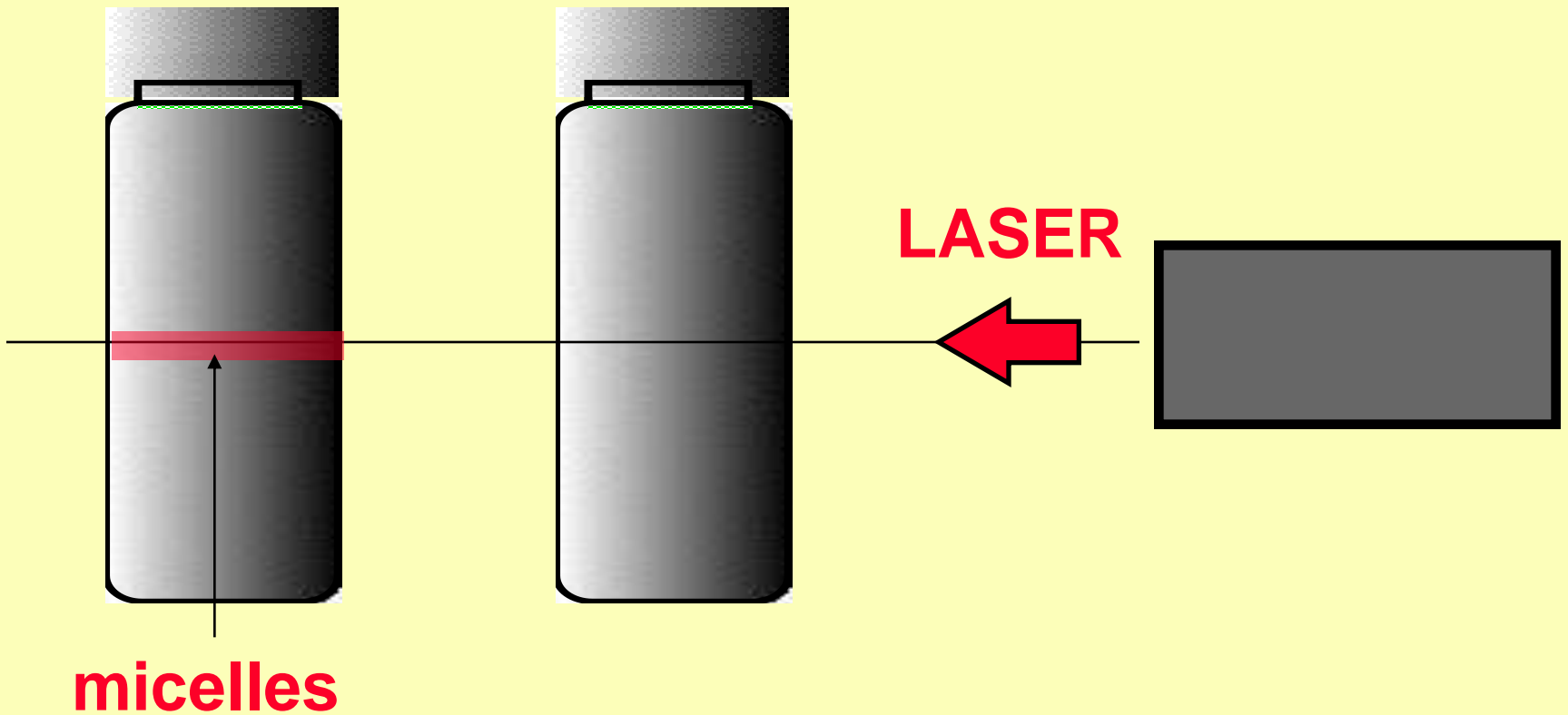
Electrolytic conductivity

(depends on the solute electrical charge)



CMC

- Laser scattering (laser)



'Critical' in CMC means a phase transition, a micro-precipitation

When $C > CMC$

- Any additional molecule goes to the micelles
- Concentration around micelles ...
- There are more micelles

... Remains constant

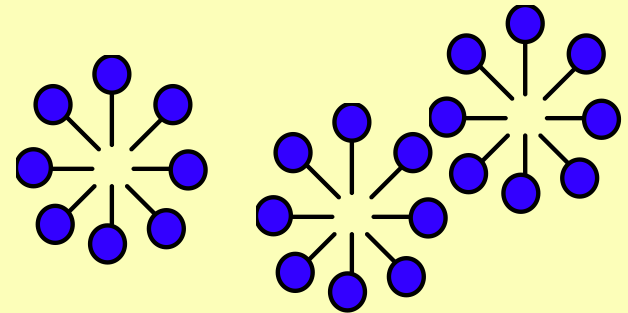
...anything that depends on it remains constant

Factors that lower CMC (favor micelle formation)

Anything that turns the surfactant more hydrophobic

- Larger non-polar group -> larger hydrophobic effect

or promotes aggregation



- Larger ionic strength
 - > lower repulsion between polar heads
- Less interaction with water (less solvency)
- Presence of an alcohol or any non-ionic additive

CMC for some non-ionic surfactants

 $\mu\text{ mol / L}$

● Octyl phenol + 1 EO	_____	45
● Octyl phenol + 2 EO		70
● Octyl phenol + 3 EO	_____	105
● Octyl phenol + 4 EO		135
● Octyl phenol + 5 EO	_____	180
● Octyl phenol + 7 EO		290
● Octyl phenol + 9 EO	_____	325

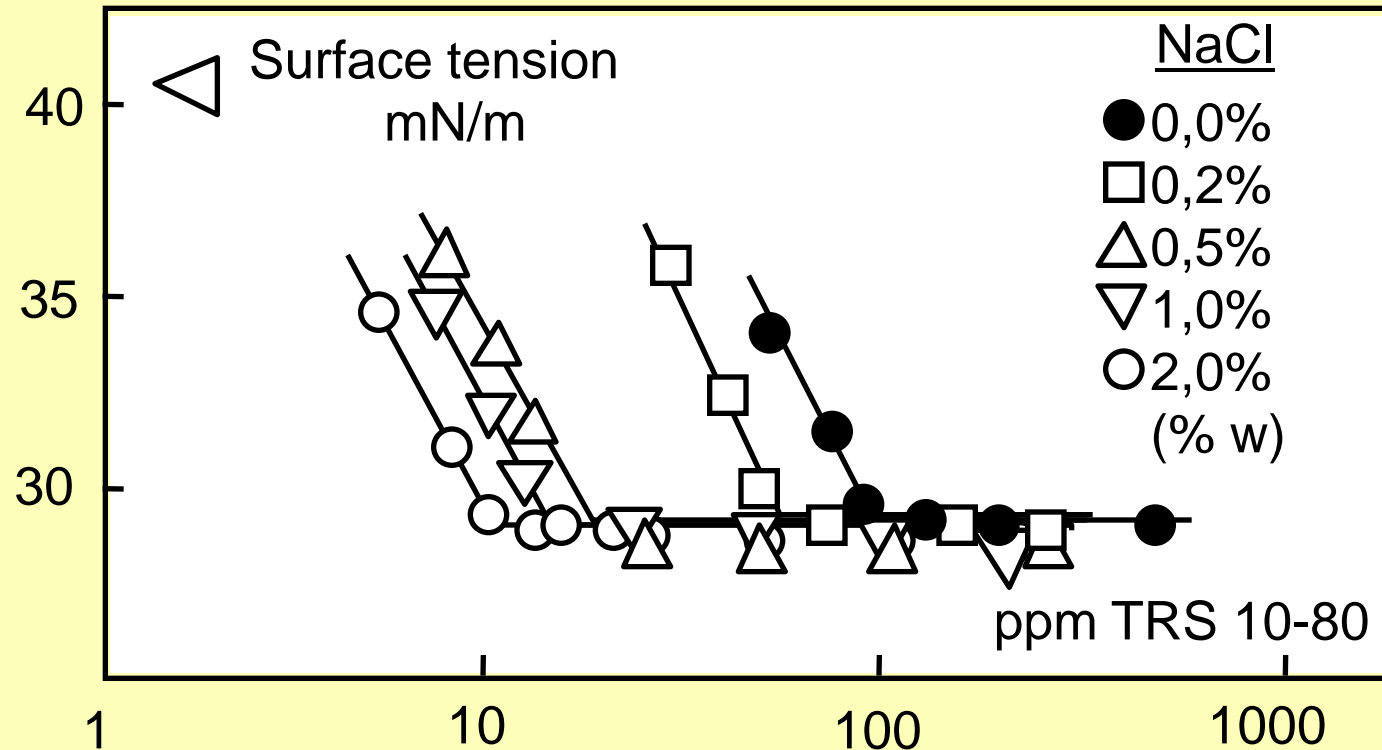
Effect of length of tail chain

CMC for some surfactants

	mmol/L
● Na Octyl sulfate	120
● Na Decyl sulfate	30
● Na Dodecyl sulfate	8
● Na Tetradecyl sulfate	2
● Na Hexadecyl sulfate	0.6
● Na Octadecyl sulfate	0.2

$$\text{Log CMC} = A - 0.30 N \text{ (carbons)}$$

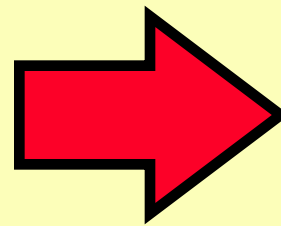
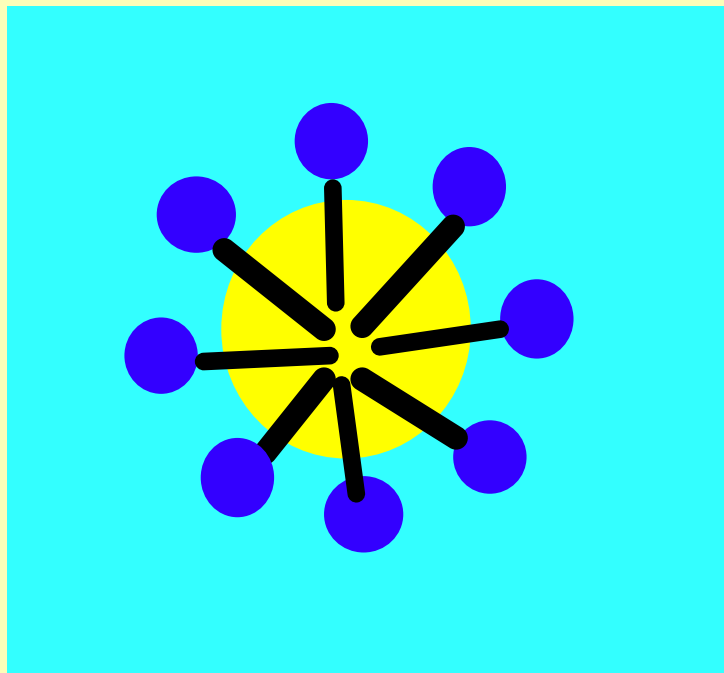
CMC as a function of salinity



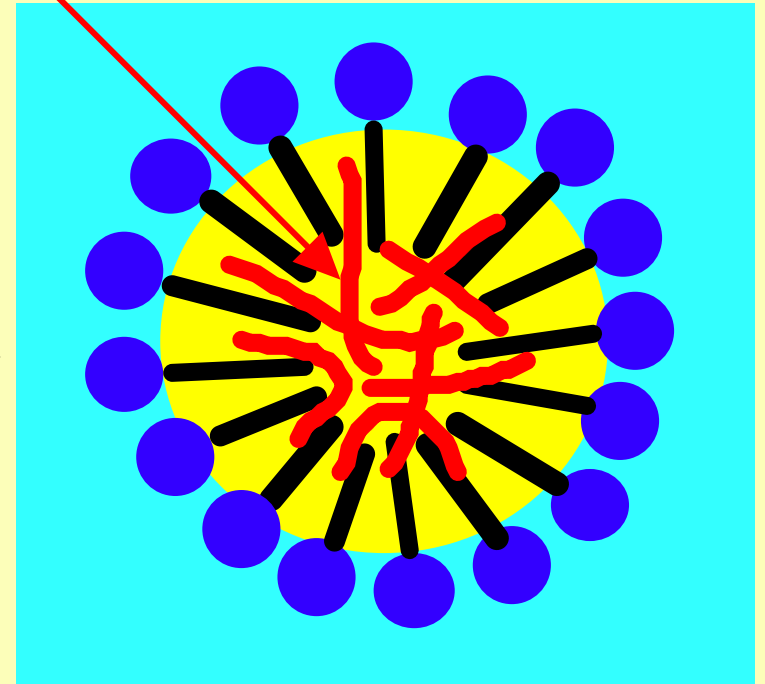
$$\log \text{CMC} = A - B \log S$$

Micellar Solubilization

oil in the core of the micelle



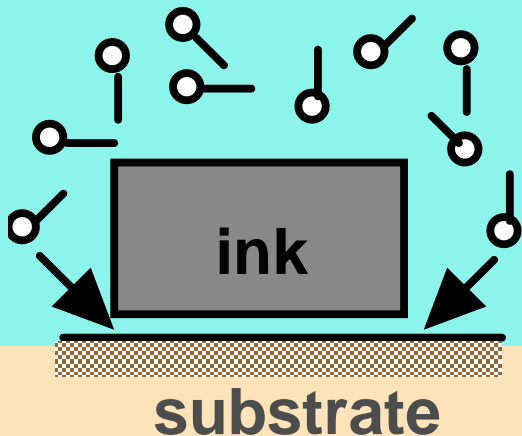
oil



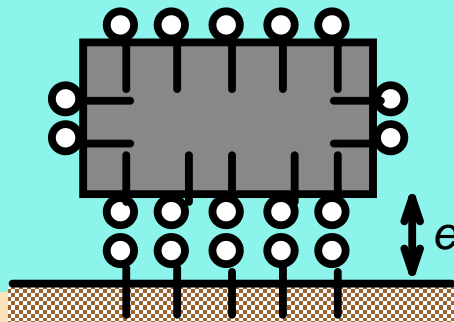
Micellization related to Detergency

“separation” of solid (ink/stickies) particle from solid and stabilized in water

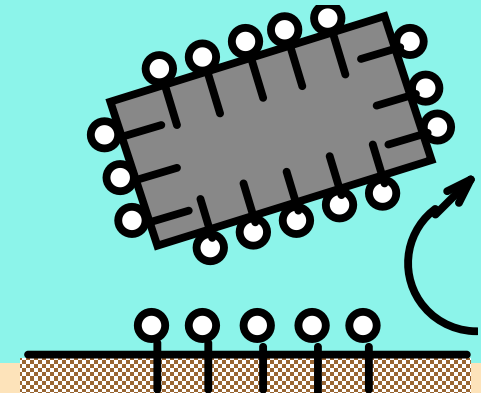
1 surfactant adsorption/diffusion



2 adhesion reduction



3 mechanical shear separation





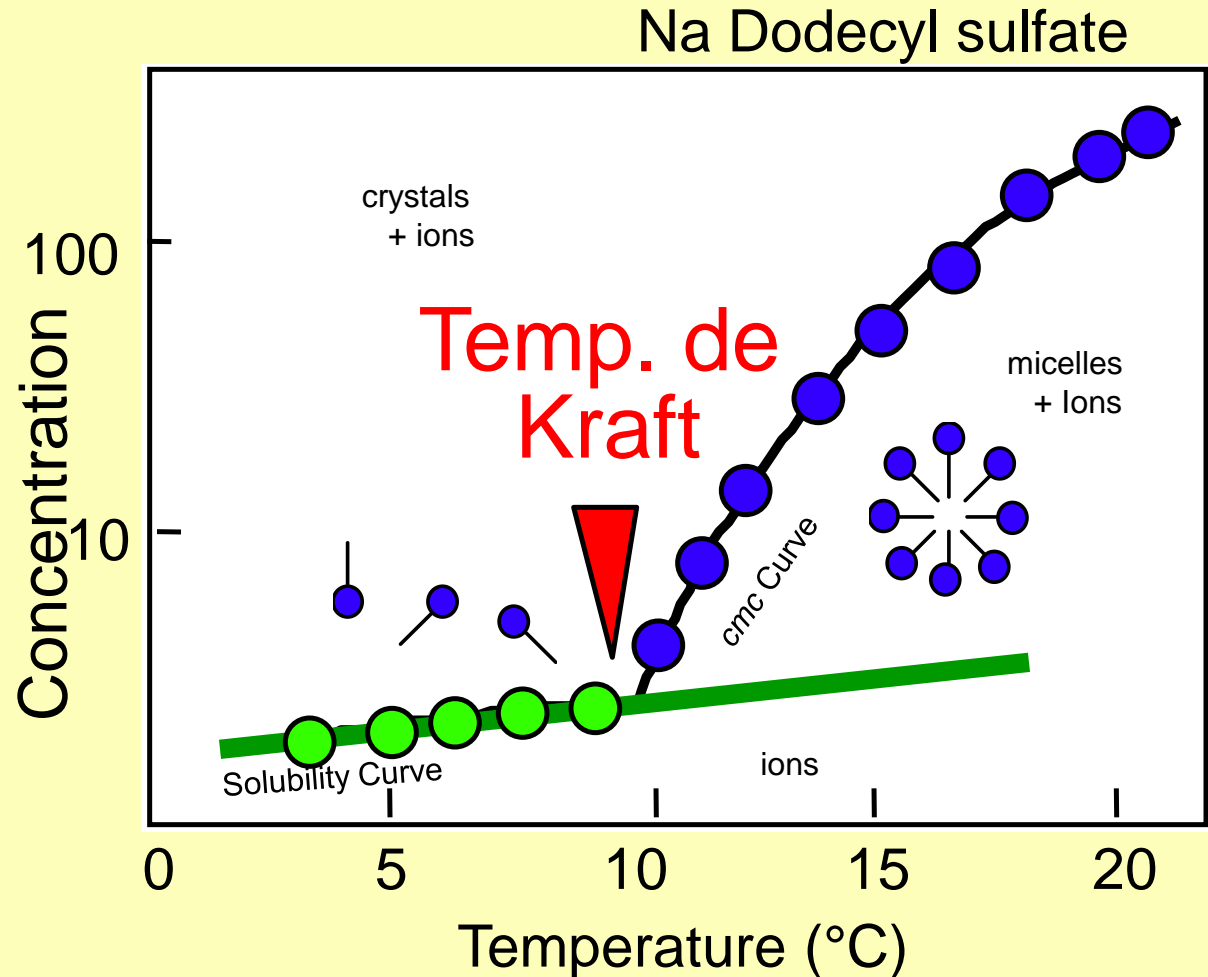
Solubility

(different than solubilization)

- *Kraft Temperature*
- *Cloud Point*

Kraft Temperature (ionics)

The temperature below which micelles do not form. Apparent solubility increases greatly above T_K .



Cloud Point (non-ionics)

- T at which the surfactant solution becomes cloudy
- This is due to de-solvation of poly-EO chain due to thermal energy/motion
- A Surfactant phase separates in the form of little drops **TURBIDITY**

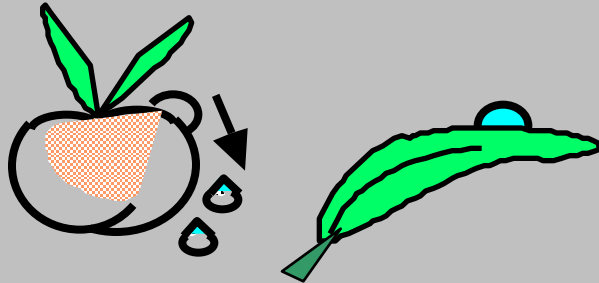
Solid Surfaces and Surface Energies



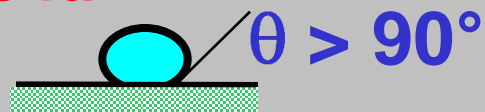


Surface modification

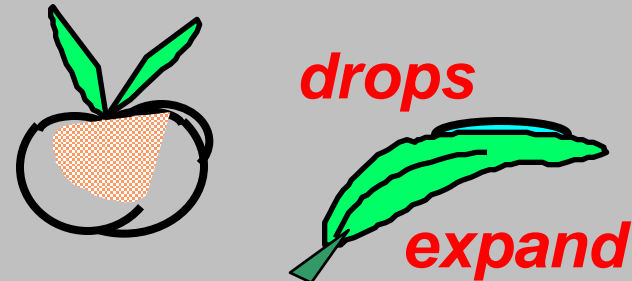
no surfactant



Drops fall
down

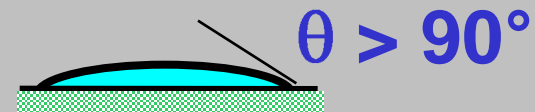


+ surfactant



drops

expand



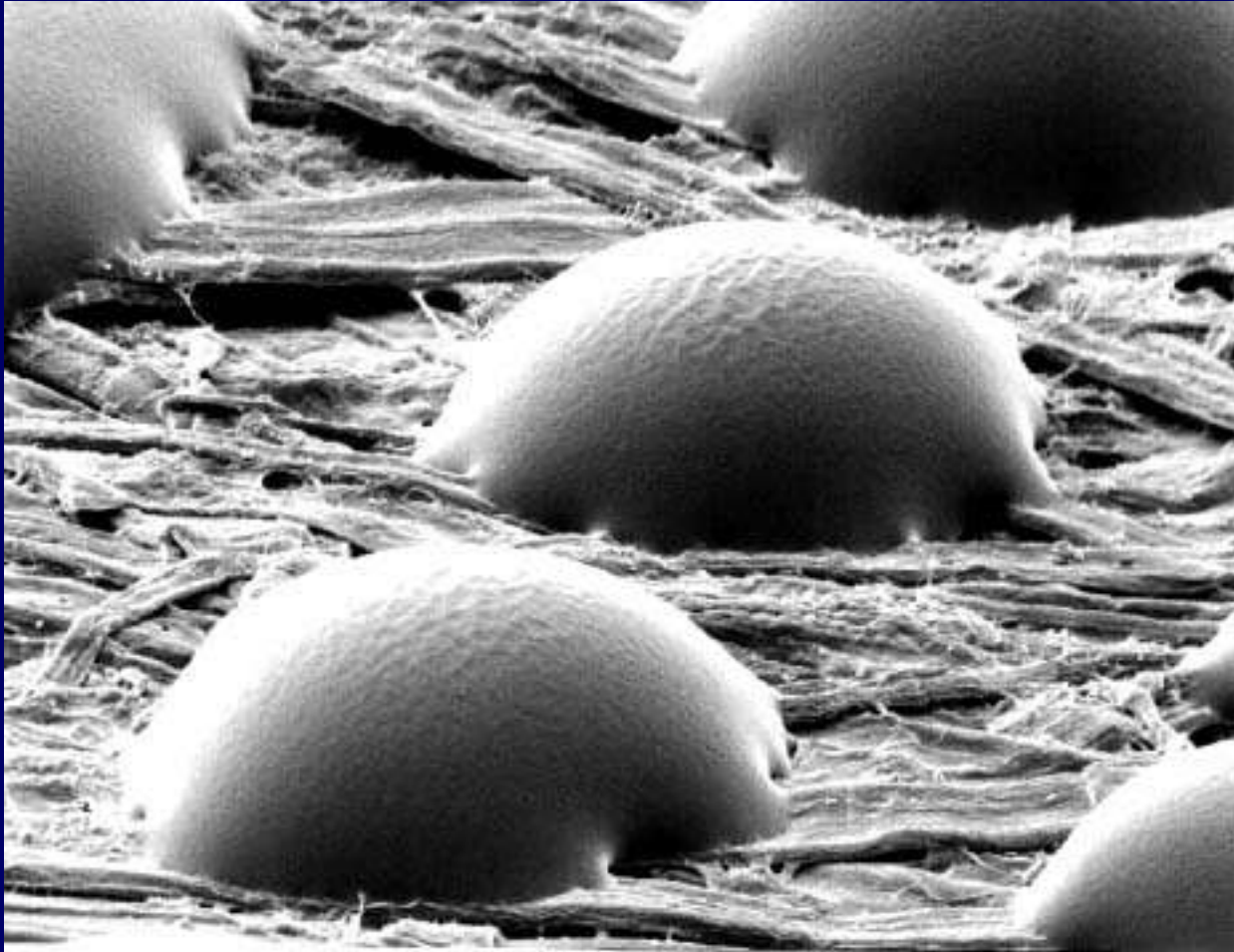
FAVORABLE



others...

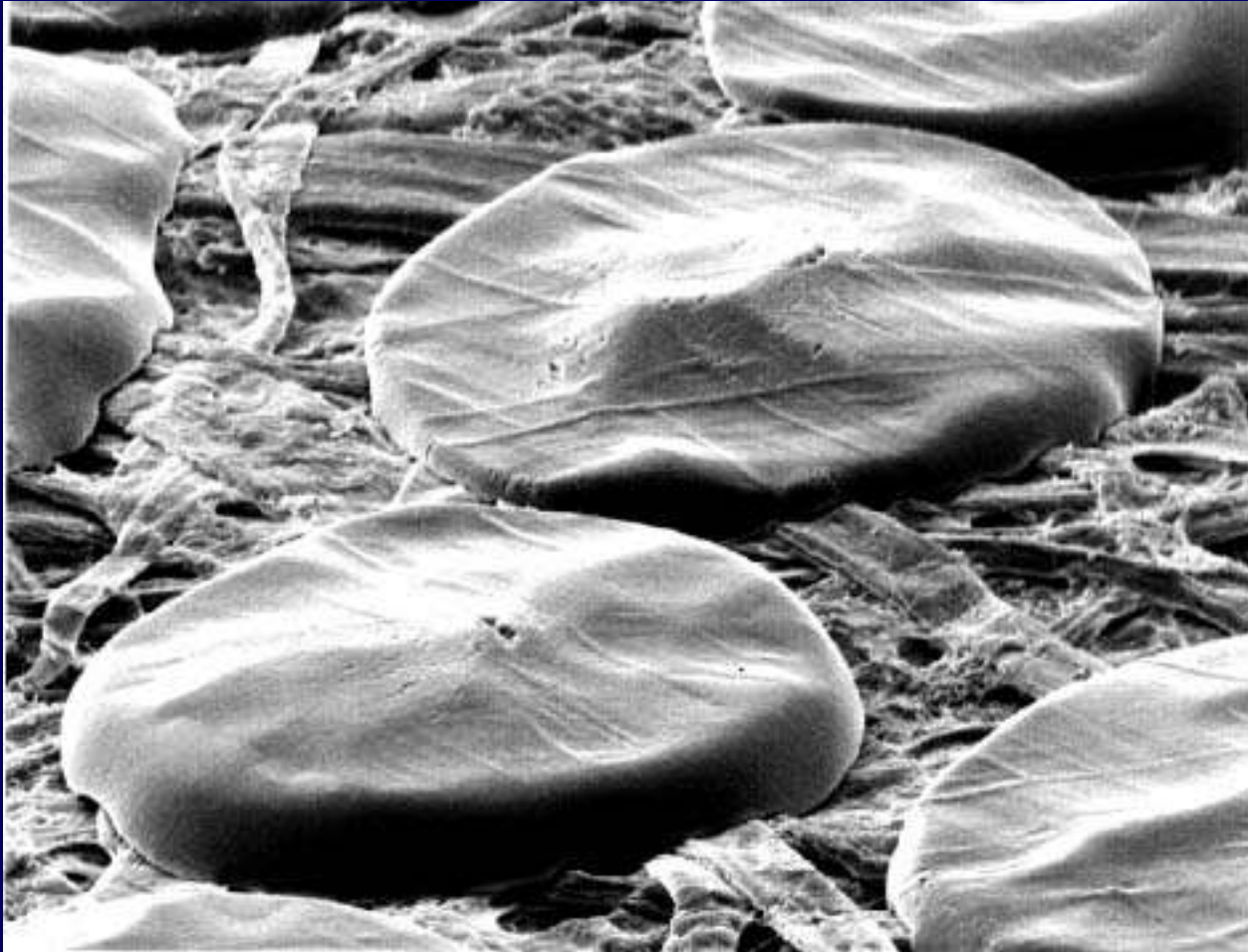


A SEM photograph of phase-change ink drops on the surface of a bond paper



Hue P. Le Progress and Trends in Ink-jet Printing Technology, Part 4
Journal of Imaging Science and Technology - 42(1), 1998

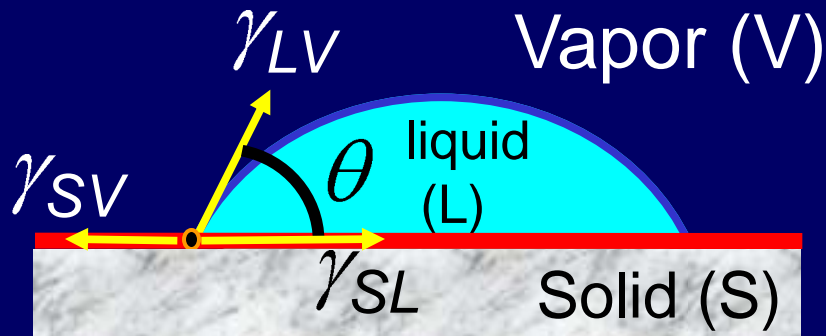
A SEM photograph of phase-change ink drops after fuse by cold pressure rollers



Hue P. Le Progress and Trends in Ink-jet Printing Technology, Part 4
Journal of Imaging Science and Technology · 42(1), 1998

Contact Angle

The concept of contact angle is rooted in the *surface energy*.



γ = interfacial tension or surface free energy

When a liquid droplet interacts with a solid surface, the droplet attains an equilibrium shape. The droplet can be characterized by the angle formed at its edge where the liquid contacts the solid surface. This angle is called the **contact angle**.

Contact Angles

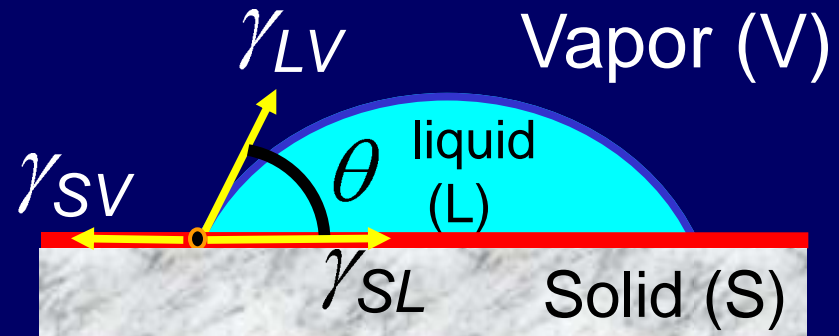
Solid	Liquid	θ
α -cellulose	water	0
	oil	0
TiO ₂	water	0
Talc	water	88
Paraffin	water	110
Polyethylene	water	95
Teflon	water	112
	mercury	150
AKD Film	water	135-140

Contact Angles for various cellulose fibers:

Pulp Type	Contact Angle
Disolved pulp; cotton	0°
Bleached softwood	20-30°
TMP (sof/hardwood)	40-50°
Unbleached softwood	50-65°
Softwood / ASA	65-90°
Softwood / AKD	60-140°
Douglas fir “self sized”	65-70°

Contact angle can be used quantitatively to measure the interaction between any liquid and solid surface. The surface free energy components of the liquid and solid can be modeled as vectors:

$$\gamma_{SV} - \gamma_{SL} = \gamma_{LV} \cos\theta$$



γ_{LV} = surface free energy of the liquid

γ_{SL} = interfacial free energy between the solid and liquid

γ_{SV} = surface free energy of the solid

This equation is derived simply from an energy balance in the horizontal direction.

Wetting can be defined based on the contact angle:

$\theta = 0^\circ$ for spreading

$0^\circ < \theta < 90^\circ$ for wetting

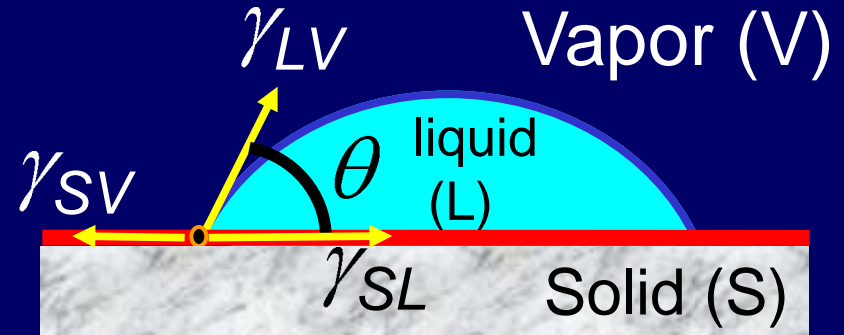
$90^\circ < \theta < 180^\circ$ for non-wetting

It is possible to have a greater thermodynamic driving force even though it is not possible to measure an angle less than zero. This greater force can be characterized by the *spreading coefficient*.

Contact angle and Interfacial Tensions

Young Eq.:

$$\gamma_{SV} - \gamma_{SL} = \gamma_{LV} \cos\theta$$



γ_{LV} = surface free energy of the liquid

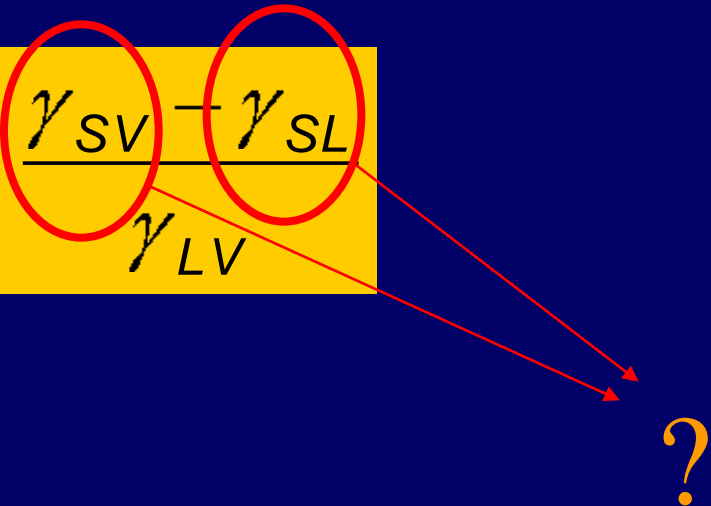
γ_{SL} = interfacial free energy between the solid and liquid

γ_{SV} = surface free energy of the solid

Let's talk about surface tension...

Solids Critical Surface Tension

Young Eq.:

$$\cos \theta = \frac{\gamma_{SV} - \gamma_{SL}}{\gamma_{LV}}$$


Surface free energy is time consuming to measure. It would be helpful if structure could be correlated with surface free energy to enable prediction of the surface energy:

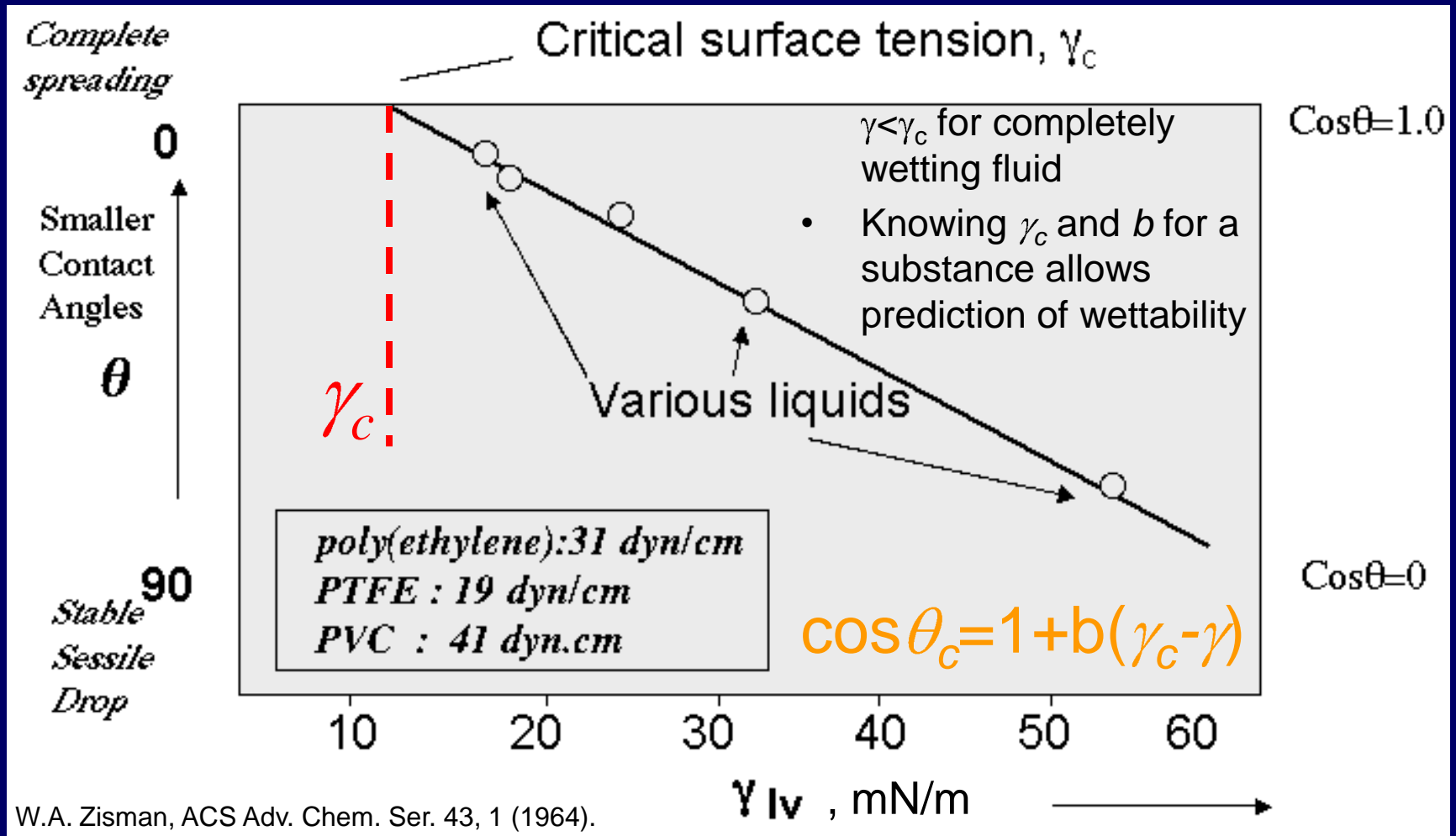
Zisman plot.

Zisman Plots and Critical Surface Energy

Cosine of the contact angle versus the surface free energy of various wetting liquids on a given solid. The resulting plot is a straight line. Thus, there exists some unique value for each polymeric solid where the cosine of the contact angle is unity. This value is termed the **critical surface free energy**. A liquid with surface free energy below the critical value will wet and spread over the solid surface, whereas a liquid with surface energy above the critical value might wet but won't spread.

Zisman Method

Critical Surface Tension



Zisman's empirical prediction fails for liquids that form hydrogen bonds or acid-base interactions with the substrate. These liquids would spread spontaneously on the substrate

Critical Surface Tension (γ_c):

Solid	γ_c (mN/m)
Teflon	18.5
Polyethylene	31
Paraffin wax	30
Starch	39
Regenerated cellulose	44
Bleached kraft pulp	34
CTMP pulp	36
AKD Film	20

Critical surface tensions

Surface groups

<u>Surface constitution</u>	<u>γ_c (mN/m)</u>
Fluorocarbon	6-25
Hydrocarbon	22-35
Chlorocarbon	≈ 40
Nitrated HC	40-45

Polymers

<u>Polymer</u>	<u>γ_c (mN/m)</u>
Teflon	≈ 18
Silicone (PDMS)	24
Polyethylene	31
PMMA, PVC	39
PET, Nylon	43

*Control wetting by surface modification;
e.g. adsorption of surfactants!!!!*

Surface Energies(*)

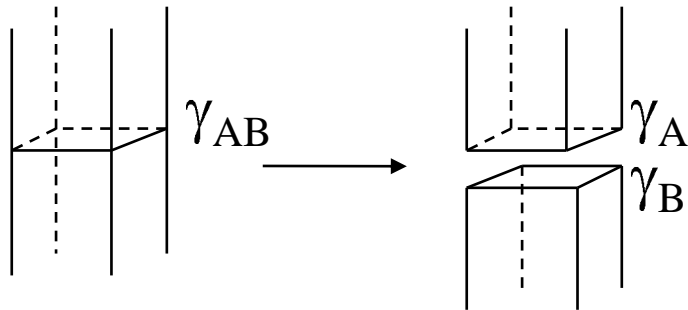
Substrate Type	Surface energy (mNm ⁻¹)	Description
Quartz (SiO ₂)* (a)(e)	25-40	Hydrophilic, acidic oxide
Poly-tetrafluoroethylene* (b)	18.5	Highly hydrophobic plastic (e.g. Teflon®)
316L stainless steel (c)	52-53	Hydrophilic, high surface energy oxide
Polyethyleneterephthalate (d)	39-61	Hydrophobic plastic (polyester)
Borosilicate glass (e)	25-40	Hydrophilic (for comparison with quartz)
Cellulose (LB-monolayer) (f)	33-36	Hydrophilic, low-charge
Wood resin(g)	25-28	Hydrophobic, extracted from wood
Gold(h)	40-45	QCM-D typical electrode, contaminant-free
Talc(i)	30-32	Hydrophobic

The critical surface tension for wetting (γ_c) is a useful interfacial parameter for comparison, though it is worth noting that γ_c is not a fundamental property of the solid and depends upon the specific (probe) liquid system [Good, W. R., "A Comparison of Contact Angle Interpretations," *J. Colloid Interface Sci.* 44 (1): 63-71 (1973)]

Surface Energies of Solids

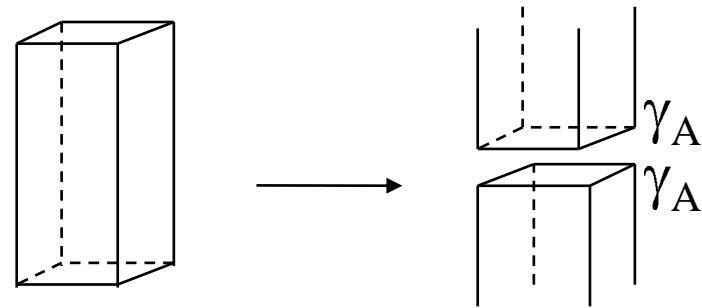
Work of Adhesion & Cohesion

Adhesion



$$W_{\text{adh}} = W_{AB} = \gamma_A + \gamma_B - \gamma_{AB}$$

Cohesion



Here, $\gamma_A = \gamma_B$ and $\gamma_{AB} = 0$, so

$$W_{\text{coh}} = W_{AA} = 2\gamma_A$$

Adhesion – state in which 2 dissimilar bodies are held together in intimate contact such that a force can be transferred across the interface.

Thermodynamic adhesion is driven by interfacial forces associated with reversible processes.

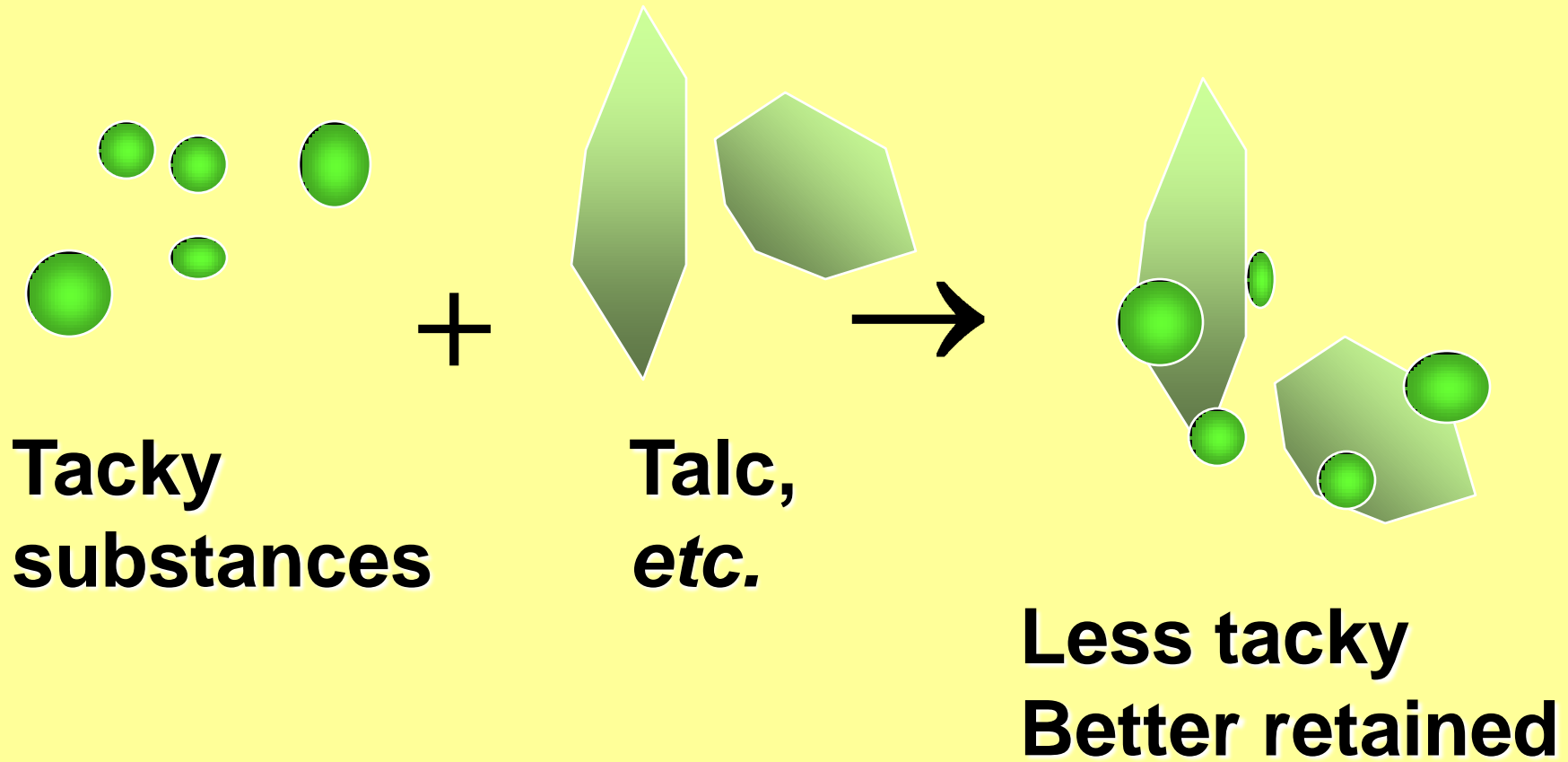
Surface Energy

In nature every system tries to minimize its surface energy.

Example: like dissolves like.

Example: hydrophobic will try to be surrounded by hydrophobic.

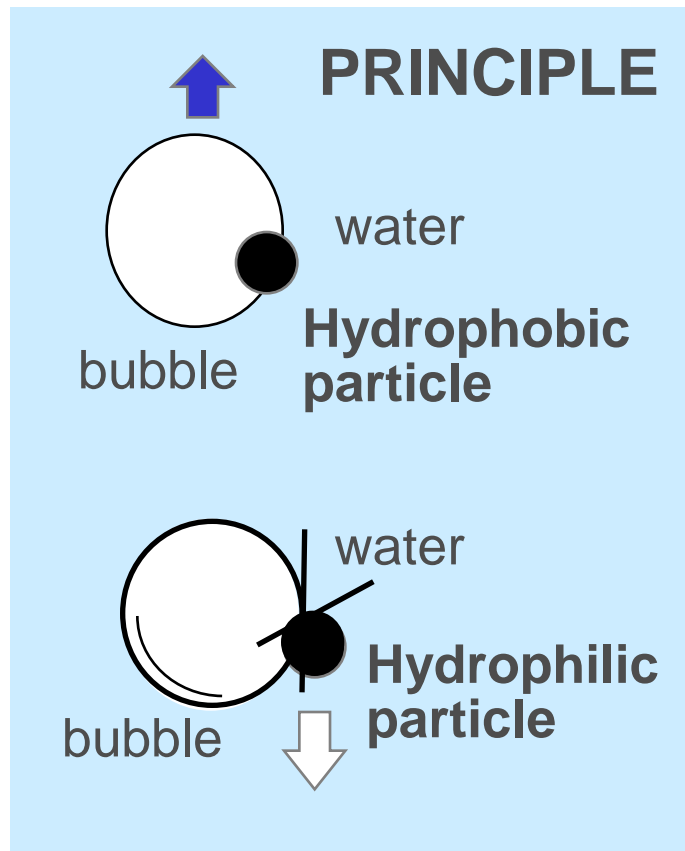
Deposits



From Hubbe

Flotation

Hydrophobic particles attach to hydrophobic air

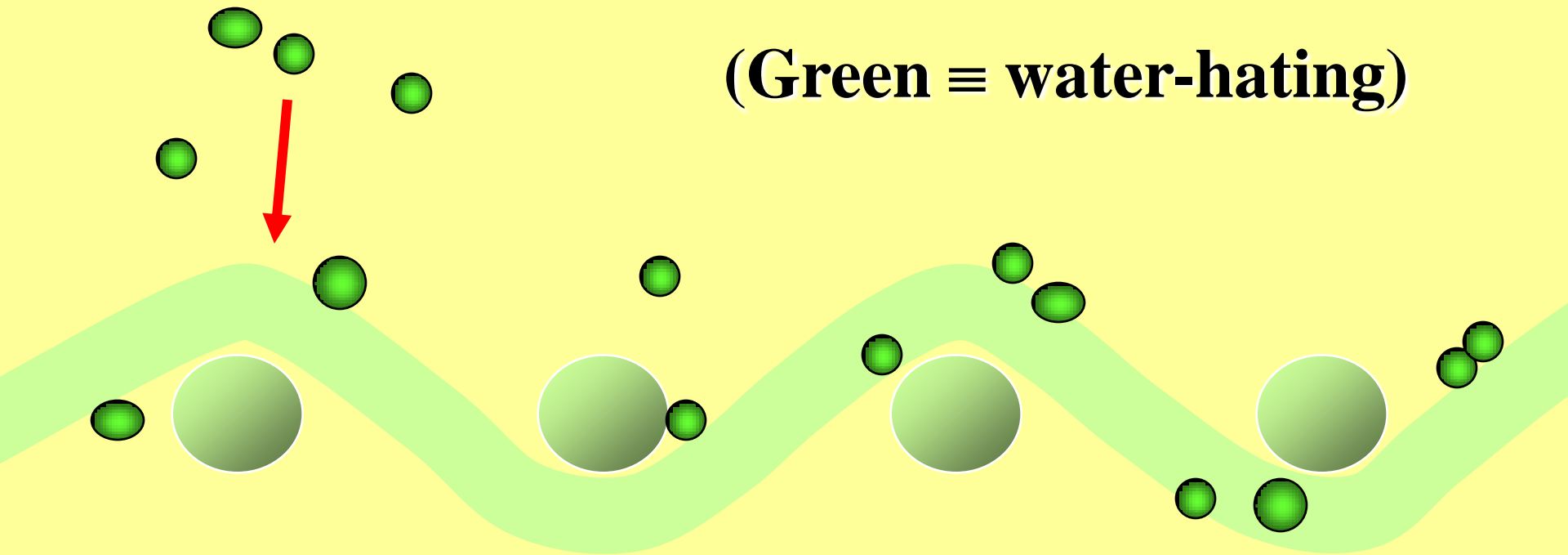


Note: the higher the contact angle between water and particle: the deeper the particle will “penetrate” the air bubble.

Surfactants work against this, actually trying to wet surface.

Stickies and deposit control

Stickies on fabrics

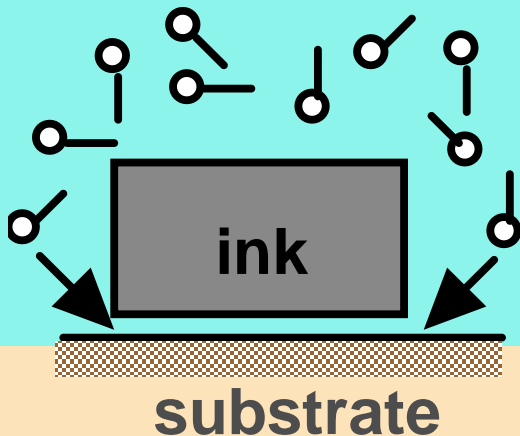


From Hubbe

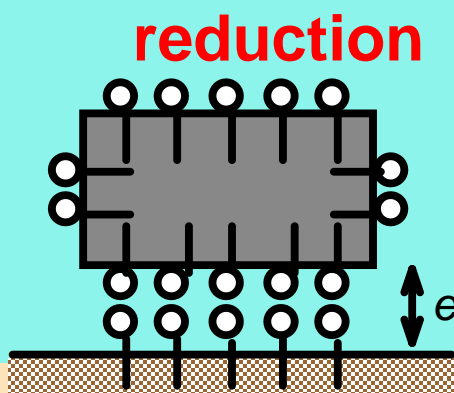
Detergency

“separation” of solid (ink/stickies) particle

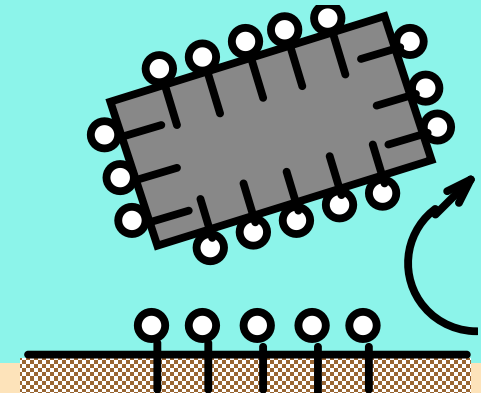
1 surfactant adsorption/diffusion



2 adhesion reduction

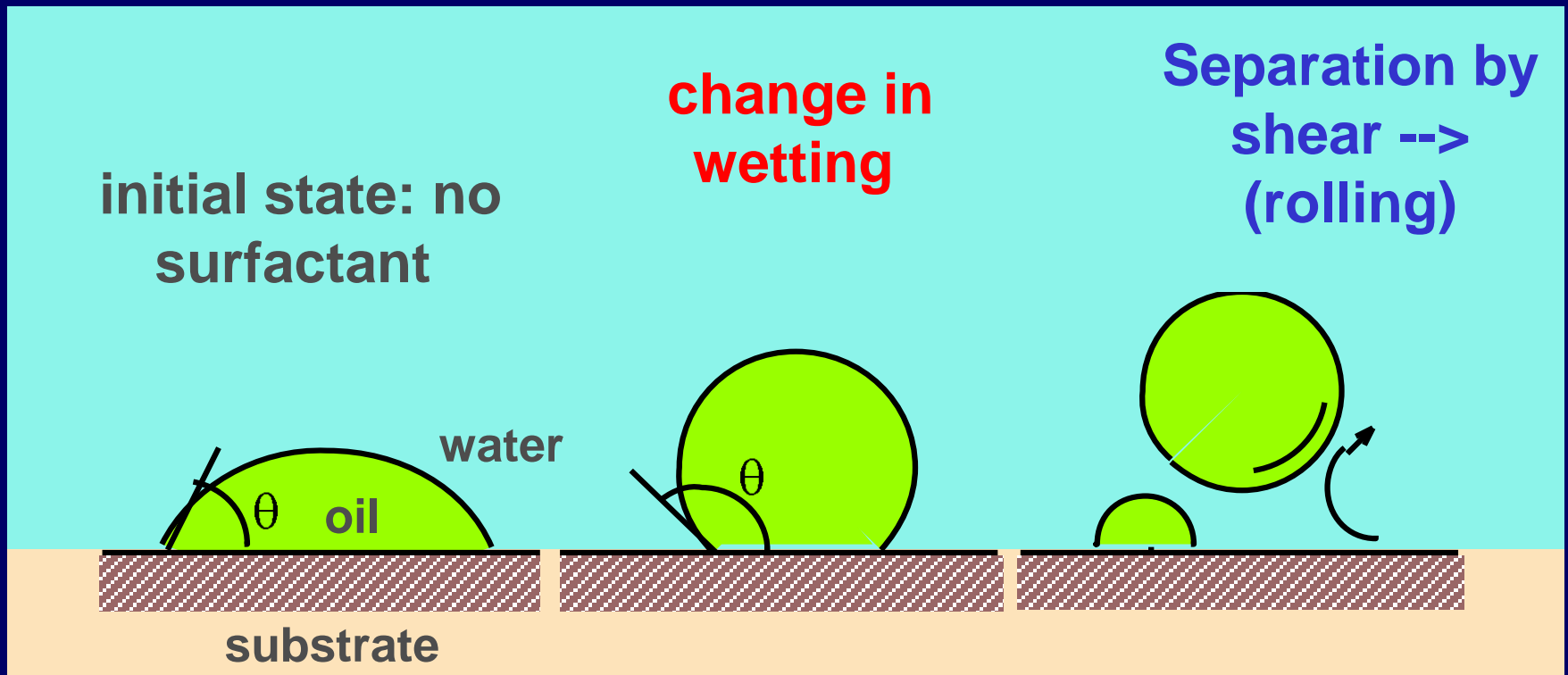


3 mechanical shear separation



Detergency

Separation of ink drop

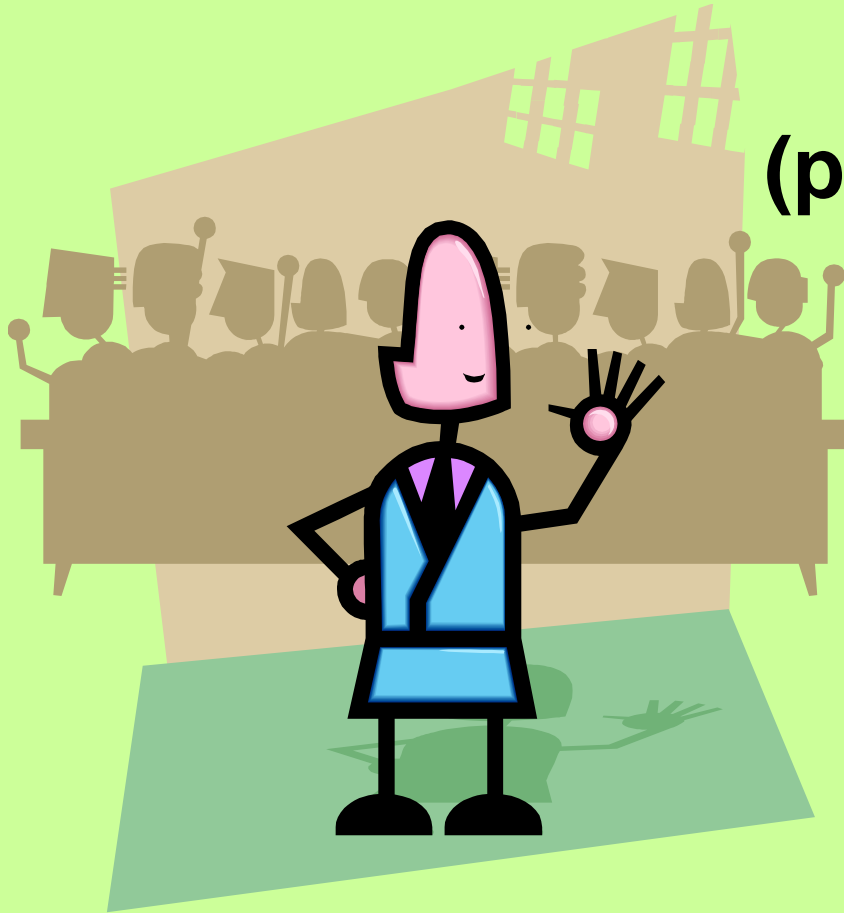


Summary

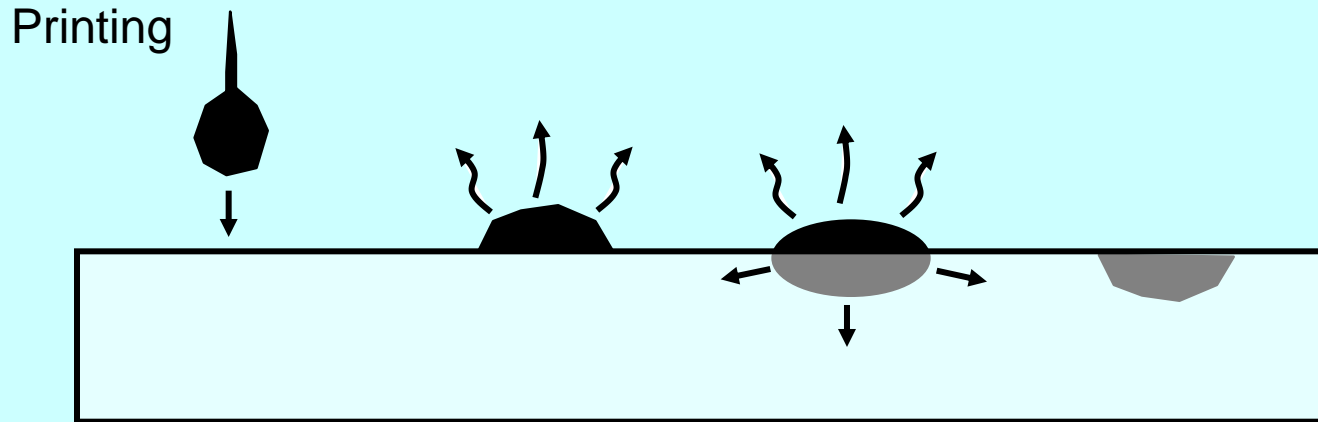
- In nature every system tries to minimize its surface energy.
- Like dissolves like.
- Surfactants have hydrophilic and hydrophobic parts
- Surfactants lower surface tension of liquids
- Surfactants will preferentially exist at surfaces, changing the surface energy of the system, affecting:
 - Foaming
 - Liquid Penetration
 - Stabilization of hydrophobic particles and liquids in water (micellization)

Liquid Penetration

(pulping, deinking,
bleaching!)



Printing = different mechanisms



Wetting Delay
& Evaporation

Wetting
Penetration &
Evaporation

Drying

Drying mechanisms of a water-based
ink-jet drop on a plain paper

Liquid Penetration

Mechanism of liquid penetration on a **paper sheet**:

- **capillary** penetration
- liquid **diffusion** in **porous media**
- **diffusion** throughout the **fiber solid fraction**

Capillary flow in paper depends on:

- **Surface chemistry (wettability)**
- **Paper structure**

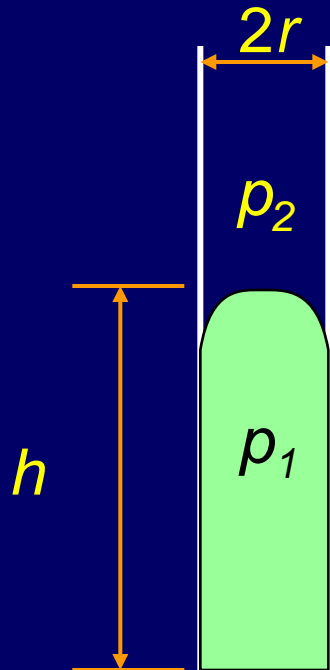
Liquid Penetration

Why is it important in pulping:

- **Water must penetrate inter fiber spaces as a prerequisite to separation of fibers**
- **Swelling of fibers (with accompanying fiber dimension changes) helps to separate ink from fiber surface**

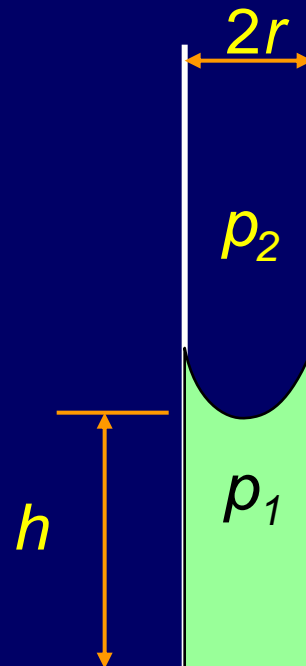
Capillary Wetting

Non-Wetting Condition



$$\theta > 90^\circ$$

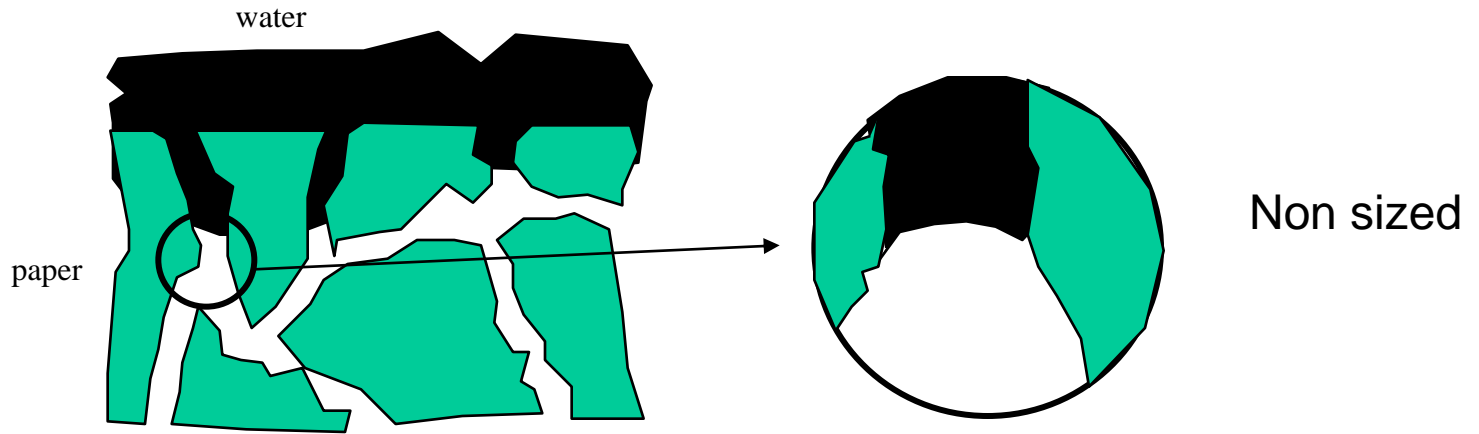
Wetting Condition






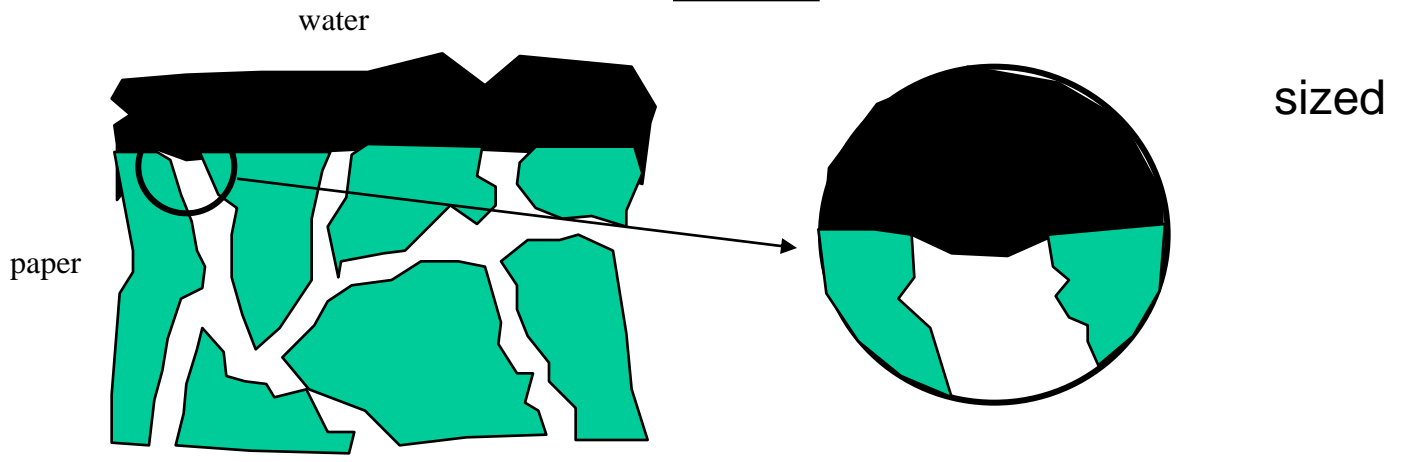
$$\theta < 90^\circ$$

$$\Delta p = p_1 - p_2$$

- Liquid enters the paper by capillary imbibition and enters the space between the fibers.
- If the liquid can cause swelling, it will also then enter the fiber walls.
- Any expansion in paper is due to water inside fiber walls and not between the fibers.
- Swelling is often just used as an expression for water absorption by the fibers, because of the resulting dimensional changes.
- This is no longer really a capillary effect although it can appear to obey the same laws.



-  Pores
-  Fibres
-  water



Interaction of Water with Paper

Capillary sorption is described by the Hagen-Poiseuille equation but this must be used carefully where swelling occurs. For a single capillary:

$$\frac{dh}{dt} = \frac{r^2 \Delta P}{8\eta h}$$

Assume paper is a set of capillaries of radius r perpendicular to the surface. The pressure caused by the meniscus of a liquid in one of these capillaries is

$$\Delta P = \frac{2\gamma \cos\theta}{r}$$

Lucas-Washburn Equation

Combining the last two equations:

$$\frac{dh}{dt} = \frac{r\gamma \cos(\theta)}{4\eta h}$$

(differential form)



$$h^2 = \frac{r\gamma \cos\theta}{2\eta} t$$

h = height of penetration up a capillary

r = radius of the capillary

t = time

γ = surface tension

η = viscosity of the liquid

θ = contact angle of the liquid and capillary wall

Internal sizing

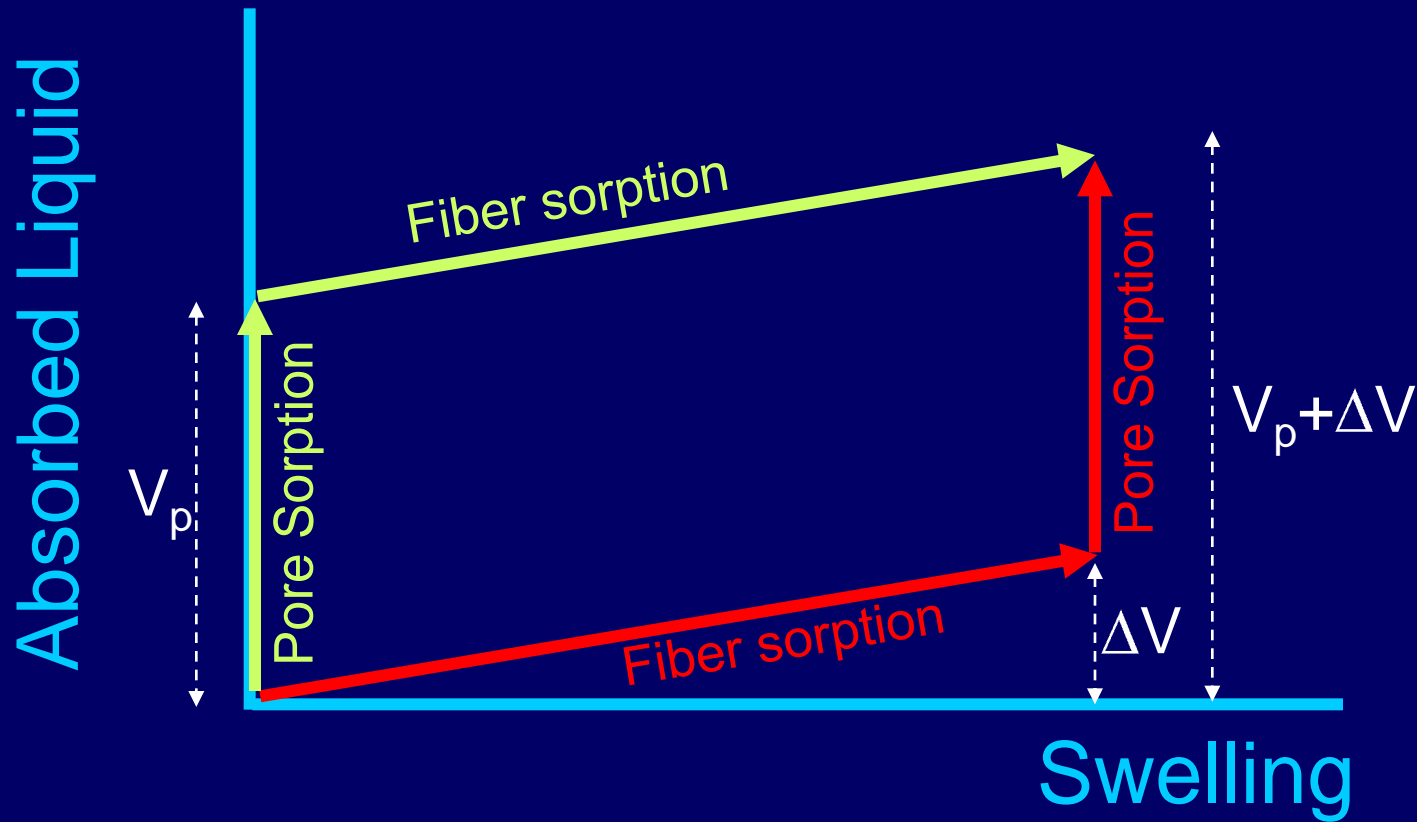
Refining/surface sizing

This tells us that the flow of water into the pores of the structure due to capillary action should be proportional to the square root of time (which is more or less a general law for porous materials).

Sorption into fibers involves capillary action but also involves surface diffusion and diffusion through cellulose. It does, however, still follow a square root law (dist penetrated to sqrt time).

The degree of intra-fiber sorption can be determined by measuring z-direction swelling and the total sorption can be determined gravimetrically, so it is possible to separate the two and express the combined system as a parallelogram model.

Sorption of water into paper



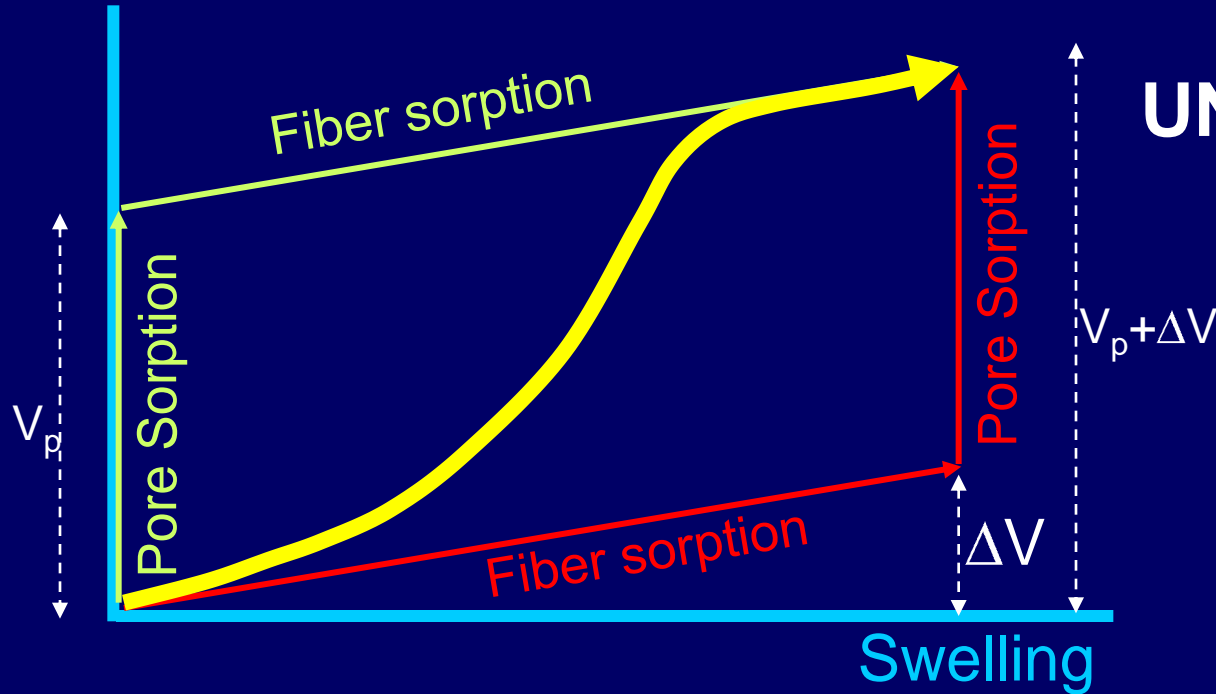
macropores are filled first followed by slower fiber swelling

fibers absorb water first followed by macropores (e.g. vapor exposure).

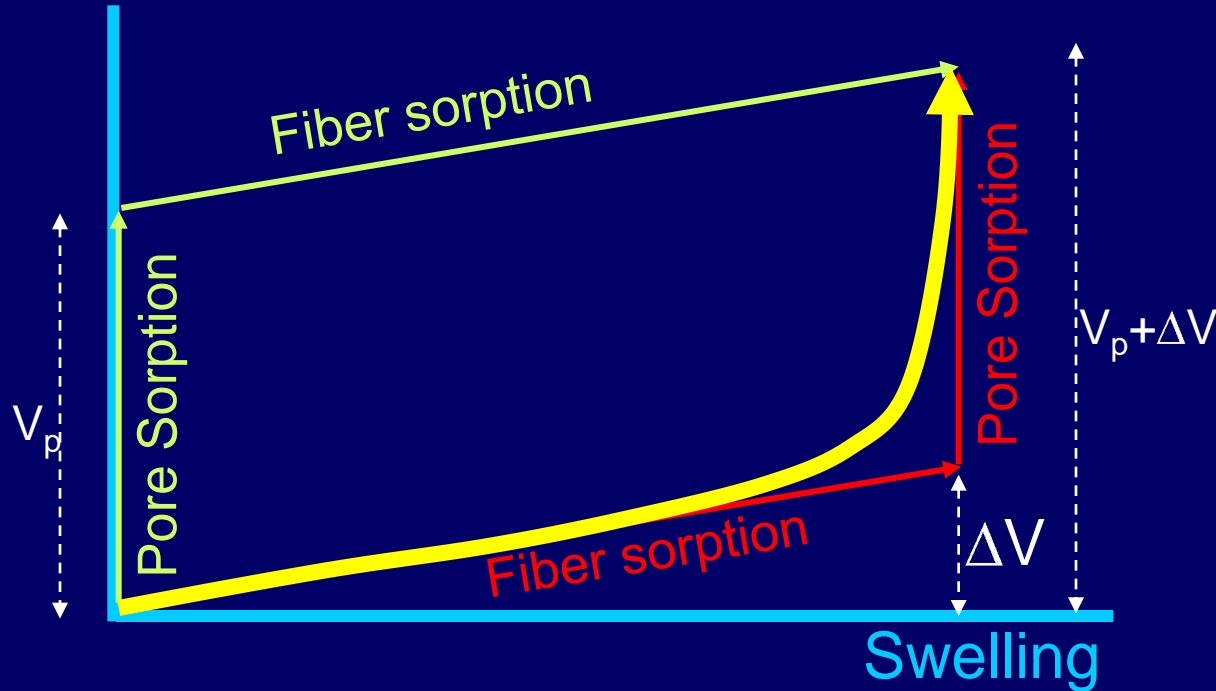
Pore sorption: absorption by capillary action into the gaps between fibers

Fiber sorption: absorption into the fibers themselves, which causes swelling.

Absorbed Liquid



Absorbed Liquid



SIZED PAPER

Sorption into the gaps between fibers is prevented. The inside of the fibers can still be filled by vapor diffusion

Summary

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